A Comparative Study of Multiple Regression Analysis and Back Propagation Neural Network Approaches for Predicting Financial Strength of Banks: An Indian Perspective

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Abstract: - The main motivation of this study is to forecast the performance of Indian banks using multiple regression analysis and artificial neural network and to compare these two methods for the accuracy. To achieve this goal, financial data spread over 10 years from 2010 to 2019 was collected from 19 Indian public sector banks. The data consists of 17 financial ratios collected from financial statements and other publications of the sample organizations. Capital Adequacy Ratio (CRAR) has been chosen as dependent variable for measuring and predicting the financial strength of banks. Identification of significant ratios that are determinants of CRAR are identified by using regression technique then these identified ratios are used as input for a developing a neural network model. The findings of multi-linear regression analysis identified 7 financial ratios that have a positive relationship between with dependent variable (CRAR). These 7 dependent variables were used to predict the financial strength (CRAR) of the Banks. Then a feed forward back propagation neural network was developed with these 7 dependent variables to predict the CRAR. Finally, the performances of these two methods were measured by using the Mean Square Error (MSE), Root Mean Squared Error (RMSE) and Mean Absolute Percent Error (MAPE). The results indicate that ANN model scores an improvement of 55.67% in MSE over regression model. In RMSE which re-scales the errors in order to keep the errors’ dimension as the predicted value, ANN model scores an improvement of 33.425% over regression model. It also indicates that ANN model scores an improvement of 99.32% over regression model in MAPE which measures the magnitude of absolute errors in relative terms. Results show that ANN model outperforms the regression model and is superior technique of forecasting CRAR of Indian Banks.

Key-Words: - Machine Learning (ML), Regression, Artificial Neural Networks (ANN), Capital Adequacy Ratio (CRAR), Financial Ratios, Financial Strength, Bankruptcy

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1 Introduction

Financial Institutions play a vital role in the economy and several studies contend that the efficiency of financial intermediation affects economic growth. Thus, the financial strength of banks has been an issue of main interest for various stakeholders such as regulators, depositors, investors, and customers. Traditionally, the financial strength of banks has been assessed on the basis of financial ratios but the advances in statistical techniques and machine learning techniques have resulted in a move towards the use of such techniques. After examining the related literature, it was revealed that multi-linear regression technique is the most commonly used statistical technique to predict the financial strength of the financial institutions. Regression technique is simple for figuring out the financial strength of the financial institutions and therefore widely used to measure the performance of these institutions. When there is no suitable mathematical relationship between independent and dependent variables, then machine learning technique of neural network can be used to get better results. Therefore, this study uses both regression and artificial neural networks (ANN) to develop models for predicting the financial stability of the financial institutions. This study has made comparison of prediction accuracy of these methods
find out the a most appropriate tool for prediction of financial strength of financial institutions.

2 Literature Review

Various studies have identified the factors responsible for the financial strength and profitability of the bank and have used these factors for measuring and predicting the performance of the banks. In a review of empirical measurements of bank performance, two broad methods: nonstructural and structural were distinguished by [1]. A non-structural approach is based on selection of financial ratios that can measure the various features of performance, whereas a structural approach usually depends on the economics of profit maximization or cost minimization. Since, this study is focused on modeling the data which is in the form of bank ratios to predict the profitability of banks, therefore, it shuns a structural approach in favor of a nonstructural one. Review of literature reveals that most of the research on finding the profitability of bank are focused on developed countries and there are only a few of studies based on developing countries [3]; [4]; [5] but most of these studies have used mostly the same variables. Several researches have used CAMEL (Capital adequacy, Asset quality, Management efficiency, Earnings performance and Liquidity) to study factors that affect the profitability of the banks [8]; [9]. CAMEL was developed by the US Federal Deposit Insurance Corporation (FDIC) for early identification of problems in banks operations. Although there are various other bank assessment models but CAMEL model has emerged as most commonly used which is even recommended by various international organizations like IMF [10]. In this study, CAMEL rating system has been chosen as a basis because it allows gauging the bank’s overall condition and performance. However, it should be noted that this system is not standardized and is very comprehensive. Due to this, it is hard if not impossible to assess the performance of the banks covered in this study. In this regard, this study has selected ratios which could serve as a substitution to certain elements of CAMEL system.

Capital Adequacy is one the important determinant of banks performance as evidenced by the literature. The issue of capital adequacy requirement originates from the work of Brechling & Clayton (1965) who raised the issue of probable existence of optimum level of owners’ equity which banks would prefer to maintain in order to ensure the stability of banks with the simultaneous effective use of available own financial resources [11]. In an empirical study conducted by Pelzman in 1970’s concluded that both the level of bank capital and its distribution would be about the same if the regulatory apparatus had never come into being [12]. Christian et al. demonstrated that capital adequacy among other variables is the most informative source for assessing banks’ returns [13]. Minimum capital requirements are being considered as the primary means of stabilizing banking sector by a growing literature. According to Basel Accord, the regulators around the world agree that capital adequacy is vital but it has been observed that nations tend to weaken this agreement by applying capital rules and regulations discriminatingly [14]. In the last few decades, Machine learning method of ANN has emerged as the widely used technique for bankruptcy prediction, fraud detection of credit cards and insurance, loan evaluation [15]. The performance comparison of ANN has been carried out with various traditional statistical methods like with multiple linear regression [17] and [18], discriminant analysis and logistic regression [19], decision trees and logistic regression [20], stepwise regression and ridge regression [21], logistic regression [22]. In almost all of these studies, has outclassed these traditional techniques. In fact, it has been established that performance of ANN is far better than multiple regression especially when the size of date is large[17]. Nowadays, ANNs are widely used to predict the bankruptcy of companies especially banks [23] [24]. Boritz & Kennedy (1995) studied various types of ANN and then compared their performance with various other traditional bankruptcy prediction methods such as discriminant analysis, logit and probit techniques [25]. In fact, results of numerous other studies that have made such comparison reveal that prediction accuracy of ANN exceeds all other methods [26]; [27]; [28]; [29]; [30]; [31]; [32]; [33]; [34]; [35]; [36]; [37]. Only advantage that these traditional methods have is that they are easy to understand and use [38]. With the above literature signifying the neural network technique in prediction of the performance of banks, this study has used both techniques in conjunction. CRAR has been chosen as dependent variable for measuring and predicting the financial strength of banks. Identification of significant ratios that are determinants of CRAR are identified by using regression techniques then these identified ratios are used as input for a developing a neural network model. In the next sections, an attempt has been made to develop a CRAR prediction model.
from the data. The model thus developed has been tested on the real data obtained from the sample organizations.

3 Selection of Variables
The data for the study was collected from 19 public sector banks from Indian banking industry. The financial data was collected from financial statements and other publications of the sample organizations. The data thus collected were analyzed through 17 financial ratios labeled from V1 to V17 as presented in table 1. The financial data spread over 10 years from 2010 to 2019 about these ratios were collected from sample organizations and analyzed through various financial tools.

4 Model Development through Regression
In order to build the model, CRAR (V1) has been taken as dependent variable, keeping in view the nature of this variable and expert opinion. Thus, Multiple Regression was run with CRAR (V1) as dependent variable and all other variables from V2 to V17 were included as independent variables to build the model. The regression was run in MS-Excel by XLSTAT with stepwise method. Stepwise regression technique attempts to find out the significant variables of a model by adding or subtracting them and consequently creates a model that is more accurate in predictions. Forward stepwise regression adds the variables on the basis of their ability to positively influence the prediction competency of the model which is primarily based on the level of significance or p-value. When a variable is added, the model is re-evaluated to find out if any other variable can be added. Once there are no more variables that can be added to the model, the stepwise regression stops and the model is used as final. This final model is then used for predicting the outcome of dependent variables i.e., output based on independent variables i.e., inputs [39].

Table 2: Regression Results

<table>
<thead>
<tr>
<th>No of Var</th>
<th>Variables</th>
<th>IN/OUT</th>
<th>Variable</th>
<th>Status</th>
<th>MSE</th>
<th>R²</th>
<th>Adjusted R²</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>V11</td>
<td>IN</td>
<td>V16</td>
<td></td>
<td>1.682</td>
<td>0.307</td>
<td>0.303</td>
</tr>
<tr>
<td>2</td>
<td>V2/V11</td>
<td>IN</td>
<td>V2</td>
<td></td>
<td>1.546</td>
<td>0.367</td>
<td>0.359</td>
</tr>
<tr>
<td>3</td>
<td>V2/V7/V11</td>
<td>IN</td>
<td>V7</td>
<td></td>
<td>1.492</td>
<td>0.393</td>
<td>0.381</td>
</tr>
<tr>
<td>4</td>
<td>V2/V7/V11/V14</td>
<td>IN</td>
<td>V14</td>
<td></td>
<td>1.393</td>
<td>0.437</td>
<td>0.423</td>
</tr>
<tr>
<td>5</td>
<td>V2/V7/V8/V14</td>
<td>IN</td>
<td>V8</td>
<td></td>
<td>1.296</td>
<td>0.476</td>
<td>0.463</td>
</tr>
<tr>
<td>6</td>
<td>V2/V5/V7/V8/V9/V14</td>
<td>IN</td>
<td>V9</td>
<td></td>
<td>1.242</td>
<td>0.501</td>
<td>0.485</td>
</tr>
<tr>
<td>7</td>
<td>V2/V5/V7/V8/V9/V14/V16</td>
<td>IN</td>
<td>V16</td>
<td></td>
<td>1.185</td>
<td>0.531</td>
<td>0.509</td>
</tr>
</tbody>
</table>

Table 3: Goodness of Fit Statistics

<table>
<thead>
<tr>
<th>Observations</th>
<th>160</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sum of weights</td>
<td>160</td>
</tr>
<tr>
<td>DF²</td>
<td>152</td>
</tr>
<tr>
<td>R²</td>
<td>0.531</td>
</tr>
<tr>
<td>Adjusted R²</td>
<td>0.509</td>
</tr>
<tr>
<td>MSE</td>
<td>1.185</td>
</tr>
<tr>
<td>RMSE</td>
<td>1.088</td>
</tr>
<tr>
<td>MAPE</td>
<td>6.433</td>
</tr>
<tr>
<td>DW</td>
<td>1.323</td>
</tr>
</tbody>
</table>

Table 2, depicts the different steps of stepwise selection of variables. The stepwise regression in our study extracted only seven variables V2, V5, V7, V8, V9, V14 and V16 that have significant effect on dependent variable CRAR(V1) out of total sixteen independent variables as significant. This model has R2 value of 0.531 and has the lowest MSE at 1.185 among all the models tested by stepwise regression, hence these seven variables have been included in the final model.

Hence the regression model is represented as:

\[ V1 = \beta_0 + \beta_1 V2 + \beta_2 V5 + \beta_2 V7 + \beta_2 V8 + \beta_2 V9 + \beta_2 V14 + \beta_2 V16 \]

4.1 Goodness of Fit Statistics
Fitting of the regression model are given in table 3.
Observations: The number of observations used is 160.

DF: Degrees of freedom or the number for the selected model is 152

R²: The R² which determines the proportion of the variance in dependent variables is 0.531.

Adjusted R²: The adjusted determination coefficient R² which is improvement to the R² takes into consideration the number of variables used in the model is 0.509.

MSE: The mean of the squares of the errors (MSE) value is equal to 1.185

RMSE: It is the square root of the MSE and is equal to 1.088.

MAPE: The Mean Absolute Percentage Error (MAPE) is 6.433.

DW: The Durbin-Watson statistic is calculated by the formula

\[
d = \frac{\sum_{t=1}^{n} (e_t - e_{t-1})^2}{\sum_{t=1}^{n} e_t^2}
\]

For better performance of a neural network, choice of proper inputs independent variables is very important. This study has used the results of regression for the proper choice of input variables. The regression model applied on the sample data in previous section identified the seven independent variables out of sixteen independent variables which have significant effect on the value of dependent variable (CRAR). Therefore, in this section a neural network has been developed using these seven independent variables. Since we have only one dependent variable, the network will have a single output. As the number of hidden neurons to include in the network is largely the result of trial and error, therefore architecture of the neural network developed in this study has only one hidden layer with five hidden neurons.

Fig1 illustrates the architecture of the feed forward back propagation neural network used for the development of prediction model in this study. This is a two layer fully connected neural network with one hidden layer. There are seven input nodes (one for each financial ratio), five hidden nodes, one output node (for the predicted CRAR), and two bias terms. Bias term for hidden units is H-Bias and for the output unit it is O-Bias. Each input is connected by arrows to all the five hidden layer neurons. The hidden units have an activation function to feed forward the value of hidden node to output layer while the output unit is sum of inputs from hidden layer neurons and bias.

The feed forward back propagation neural network training can be summarized in the following steps as shown in fig 1:

1. Initialize the weights of the network including weights of seven inputs (V2, V5, V7, V8, V9, V14 and V16) to hidden layer and weights of five neurons (N1, N2, N3, N4 and N5) to output layer. Bias for the hidden units H-Bias and bias for the output unit it is O-Bias are also initialized.

2. Apply the input vector to the network input.

3. Calculate the output of the network based on the initial weights and input set.

4. Calculate the square error between output (Predicted V1) and the desired output (Actual V1).

5. Repeat the step 2-4 for each vector in the training set.

6. Calculate the Sum of Square Error of all the vectors of training set.
7. Propagate error backward and adjust the weights and bias terms of input to hidden layer and hidden layer to output layer in such a way that minimizes Sum of Square Error.

8. Repeat steps 3-7 until the error for the set is lower than the required minimum error.

The data consisted of seven ratios that were found to be significant determinants of dependable variable i.e., CRAR (V1) through stepwise regression in the previous chapter. Since the sample organizations considered for this study are nineteen and the spread of data is ten years, therefore, total observation are 190. Out of these 190 observations, 160 observations have been used as training data set and rest 30 observations as testing data set. The training data set consisting of 160 observations is presented in columns A through J of the spreadsheet as shown in fig 2. Since the objective of this study is to develop a NN model that can predict the CRAR of the sample banks for next year on the basis of value of independent variables of the current year. Therefore, in order to train the NN perfectly, the value of actual CRAR (V1) of every observation is one year ahead.

5.1 Feed Forward Back propagation ANN (With Exponential Activation Function)
The data in fig 2 of the ANN is explained below.

- **Input Layer:** Columns D to J represent the selected seven ratios of the sample banks. The Cells D2 to J161 contain 160 observations of data that are fed into the neural network.

- **Hidden Layer:** Columns K to O represent the selected five hidden neurons ANN. Value of neurons is calculated by exponential activation function

\[ f(x) = \frac{1}{1 + e^{(net)}} \]

where \( \text{Net} = H_{Bias} + \sum_{i=1}^{n} w_i n_i \)

For neuron1(N1), seven weights of input variables between the nodes in the input and hidden layer of the ANN are stored in cells S2 through Y2 and bias stored in Cells Z3. For neuron4(N4), seven weights of input variables between the nodes in the input and hidden layer of the ANN are stored in cells S3 through Y3 and bias stored in Cells Z3. For neuron3(N3), seven weights of input variables between the nodes in the input and hidden layer of the ANN are stored in Cells S3 through Y3 and bias stored in Cells Z3.

- **Output Layer:** Cells S9 through X9 represent the weights and cell Y9 represents bias between the nodes in the hidden and output layer. Again, weights and bias values are adjusted to zero in these cells and their optimal values will be determined later. The values of the output node for 160 observations P2 through P161 is calculated by the following equation.

\[ V_1(\text{Pred}) = O_{Bias} + \sum_{i=1}^{n} w_i n_i \]

Ideally, value of predicted V1 in cells P2 through P161 should match the value of actual V1 stored in cells C2 through C161 but since initially we have adjusted the value of weights and bias to zero therefore Predicted V1 of all 160 observations is zero.

- **Sum of Square Error (SSE):** Column P computes the squared error between the predicted output V1 and the actual value (V1) for each observation.

\[ \text{SSE} = \sum (V_1(\text{Predicted}) - V_1(\text{Actual}))^2 = \sum (y-y)^2 \]

The SSE is returned in cell Y9.
After the basic ANN model is put in place, the next step is to run each of the observations through the ANN. It is important to note that as in regression, it is necessary to determine the weights for the ANN that minimize the sum of squared errors to the least. Cognizance has also been taken of that the values of weights and biases are dynamic i.e., if there is change in the values of the weights and the value of computed hidden nodes then output i.e., V1 (Predicted) will be automatically updated. The back-propagation NN typically computes the optimal weights for an ANN which is implemented in this study through Solver.

5.2 Training the Neural Network

In this study a macro (RAF) has been recorded that runs the solver to train the neural network on training data of 160 observations with preset settings as shown in fig. 3.

Solver determines the maximum or minimum value of one cell by changing other cells. In this study, main objective is to minimize the sum of square errors i.e., cell Y9 by changing the weights and biases of input nodes and hidden nodes which is achieved in this study by using solver. These weights are stored in cells S2 through Z6 and S9 through X9. By minimizing the sum of square error, the neural network is trained to minimize the difference between V1 (Predicted) and V1 (Actual), thereby increasing the accuracy of ANN.

As shown in fig. 3, cell SY9 is set as objective and since our goal is minimization of the objective, therefore, Min. check box is selected. In the ‘By Changing Variable Cells’ box, cell range of weights and biases i.e., $S$2: $Z$6, $S$9: $X$9 is entered. In the ‘Subject to the Constraints’ box, we have set the constraint that the value of cell range of weights and biases i.e., $S$2: $Z$6, $S$9: $X$9 $S$9: $Y$9 must be between -50 to 50.

The Generalized Reduced Gradient (GRG) method is used for optimization of solution in this study. As shown in fig. 4, the constraint precision box is used to decide how close the Solver's result should be to the constraints before stopping. In this study, value of 0.0000001 is used as constraint precision. Automatic scaling is selected which causes the model to be rescaled internally before solution. It adjusts the range to each variable cell instead of using a single scale for all the variables which results in the optimal solution.

As shown in fig. 5, the convergence rate is set to 0.0000001 which controls the solver search to the optimal solution.
Require Bounds on Variables option is selected as it speeds up the process of finding the solution by limiting the array of values to lower and upper bounds that the Solver must explore.

The forward derivative tries to discover the optimal solution. It guesses the first derivative at a point by disturbing the point once in a forward direction and computing the rise over the run. Central approximations are obtained by disturbing far from the point in both backward and forward directions to compute the rise over the run. Central differences deliver a further precise guess of the derivative, but it takes double number of computations that means it twice slower.

5.3 Training Results

Both options were tried in this study and the results are depicted in table 4. Initially the Sum of Square Error was 25912.95. Which was reduced to 103.9 after solver was run three times using forward derivative approach. There was marginal reduction in error after the second run. However, central derivative approach provided better results by reducing the error to 84.02 in second run only. There was no reduction in error in the subsequent runs. Therefore, central derivative approach is selected in this study.

Table 4 presents generated weight matrix of hidden layer of the developed neural network model. The W2, W5, W7, W8, W9, W14, W16 represent weights of input nodes to five hidden neurons and BIAS represents the bias values to five hidden neurons.

Table 5 represents the fitness of good statistics of the developed model using central derivative approach. R2 value of 0.78 is significant and indicates that there is a strong correlation between independent variables and dependent variable (CRAR).

5.4 Testing the Neural Network

The trained network was then tested on the testing data of 30 observation of the sample banks to check the robustness and accuracy of the developed NN model.

Comparison of training and testing results is presented in table 6. R2 value of testing data was 0.731 which vary by 6.4% only but within the accuracy limit of ±10%. MAPE shows and improvement of 42.8% over training data. This testing result indicate the reliability and robustness of the developed model.

<table>
<thead>
<tr>
<th>Table 4: Training Results</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Derivative Method</strong></td>
</tr>
<tr>
<td>Forward</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td>Central</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 5 : Error Measurement</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>MSE</strong></td>
</tr>
<tr>
<td>0.5251</td>
</tr>
</tbody>
</table>

6 Conclusion

CRAR was selected as dependent variable as literature signifies the relevance of this ratio for measuring the performance of banks. The financial data used for development of models consisted of seventeen financial ratios of nineteen public sector banks and spread over ten years was collected from Indian banking industry. Out of seventeen ratios, seven significant ratios were identified as determinants of CRAR by stepwise regression technique. These seven ratios were used as input for developing neural network model.

The regression model was used to supplement the ANN models by using its results for the proper choice of input independent variables. A comparison of the forecasting accuracy of regression model with the chosen ANN model is presented in table 7. It provides some insight into their performance and efficiency. Four common criteria of error measurement were used to compare the two models: Mean Square Error (MSE), the Root Mean Squared Error (RMSE), the Mean Absolute Percent Error (MAPE) and the R2. The table clearly suggests that the neural network is
more accurate than the linear regression model for the type of financial data used in this study.

The MSE is a measure of overall accuracy that gives an indication of the degree of spread. It is the most common measure of forecasting accuracy. Table 7 indicates that ANN model scores an improvement of 55.67% in MSE over regression model. In RMSE which re-scales the errors in order to keep the errors’ dimension as the predicted value, ANN model scores an improvement of 33.425% over regression model. It also indicates that MAPE which measures the magnitude of absolute errors in relative terms also indicates that ANN model scores an improvement of 99.32% over regression model.

Table 7: Comparison of techniques

<table>
<thead>
<tr>
<th>Technique</th>
<th>MSE</th>
<th>RMSE</th>
<th>MAPE</th>
<th>R²</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regression</td>
<td>2.025</td>
<td>1.088</td>
<td>6.432</td>
<td>0.530</td>
</tr>
<tr>
<td>Neural Network (Exponential Activation)</td>
<td>0.525</td>
<td>0.724</td>
<td>0.043</td>
<td>0.780</td>
</tr>
<tr>
<td>Difference</td>
<td>0.659</td>
<td>0.364</td>
<td>6.389</td>
<td>0.249</td>
</tr>
<tr>
<td>%age Improvement in Error</td>
<td>55.67</td>
<td>33.425</td>
<td>99.32</td>
<td>47.041</td>
</tr>
</tbody>
</table>

Better values of MSE, RMSE and MAPE clearly indicate that neural network model is better than the regression model. R² improvement of 47% clearly shows that the neural network model is a better fit when compared to regression model. This also indicated that neural networks are better at capturing relations between input and output variables of financial data used in this study. Fig.6 clearly depicts that ANN model outperforms the regression model and is superior technique of forecasting CRAR.

6.1 Future Work and Recommendations

- The models proposed in this reports are developed by using data of 19 public sector banks of India, therefore all the results were obtained with a limited data set with limited parameters. As a recommendation, by using larger data sets and additional parameters the models can be further improved.
- Moreover, time spread of sample data can be increased as this study is based on 10 years data only.
- More kinds of different input like GDP, exchange rates, share price value etc. to the neural network model presented in this study may be considered for evaluation to ascertain whether better predictions can be made.
- Also, as a future work, performances of regression, and neural networks models developed in this study can be compared with the financial data of organizations of other types of sector such as IT, Manufacturing, Infrastructure, Services etc.
- The models developed in this study for prediction of CRAR of public sector banks, can also be used for the development of other predictive models like stock market.
- This study has used regression and neural network techniques for the development of prediction model for CRAR. Other machine learning techniques like Support Vector Machine (SVM), Genetic Algorithm etc. can be applied to this type of study and results can be compared with NN model developed in this study.

Acknowledgement

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