Optimization of a Vendor Managed Inventory Supply Chain Based on Complex Fuzzy Control Theory

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Abstract: This paper recommends a scaling factors fine-tuning fuzzy logic control approach to optimize the dynamic performance of one typical vendor managed inventory supply chain with automatic pipeline, inventory and order based production control system(VMI-APIOBPCS), based on complex fuzzy control theory. The first thing is to embed a dual-input single-output fuzzy logic controller into the system based on the classic control engineering model. Then, the fuzzy inputs are given different weights by the way of scaling factors in order to optimize the system further. This methodology can make good use of managers' experience accumulated in perennial practice and the managers' rational estimation of different circumstances. Lastly, the simulation results show that, this method can improve the dynamic performance of VMI-APIOBPCS, especially the inventory dynamic behaviors.

Key-Words: VMI-APIOBPCS, fuzzy logic controller, scaling factors, dynamic performance

1 Introduction

With the progress of the information technology the urge of mutual benefit, orgnizations (suppliers, manufacturers, distributors, wholesalers, retailers) in supply chain accommodate their strategies to this new collaborative work tendency[1]. The operational pattern of VMI come into being at the opportune historic moment. As one of the most prevalent integrated styles, the implementation of its effective control is pressing to build modern manufacturing system. However, owning to the intrinsic complexity and turbulent market changes, the effective controlling became unrealistic[2, 4]. Many factors, such as forecast error, the block of information delivery, demand change etc., always result into unexpected overstock and incremental of overall running cost[3, 5, 6, 7, 8, 12].

Those problems, existed in VMI system, are severe in other classic production and inventory control system[11], likewise, which have been discussed heatedly both in practical management and academic field for decades. Early in 1982, Towill adopted control engineering method to optimize the IOBPCS (inventory and order based production control system) by setting the proportion of inventory adjust time(Ti) and production delay(Tp) and the proportion of demand forecast smoothing time(Ta) and production delay(Tp), respectively[3]. Later, GA was employed to optimize three control parameters (Ta, Tw, Ti) of APIOBPC- S, based on stability and robustness of system, and especially, considered the work in progress(WIP) adjust time (Tw) in the optimization, a beginning of taking the production and inventory control system as an whole picture[5]. S.M.Disney, based on the research achievement in 2000, synthesized six parameters (Ta, Tw, Ti, Tq, G, W) of VMI-APIOBPCS and made an simulation optimization[6]. The centralized management method, VMI was adopted in this paper to make the manufacturer of APIOBPCS pay more attention to the integrated benefit, thus the distributor's forecast smoothing time (Tq), the proportion of Distributors Safety Stock and Average consumption (G) and Ratio of production adaptation to inventory cost(W) were considered. In conclusion, the optimization methods mentioned above simply adopted mathematical arithmetic, only reached an ideal combination of control parameters in the mathematical sense.

Although, we researched production-inventory system all-around by the classic control engineering method and came up with numerous of optimization outcomes[19, 20, 21, 23, 28], many supply chains, reported worldwide, still suffered from bad supply chain performance[7]. This situation reminds us to give deep thought about this research angle.

Actually, many researchers investigated this issue in different points. White utilized proportionintegration-differentiation (PID) controller to optimize the IOPBCS, and greatly reduced the inventory level[16]. B. Samanta combined PID controller with fuzzy logic controller to optimize an inventory control system[18]. At last, the system is capable of preserving the final system inventory level at the desired level in spite of variations in demand. However, the PID controller is not welcomed in the productioninventory research field for its congenital drawback that its corresponding hard wares is not existed in virtual production-inventory systems[7].

As regards to the control of inventory and production system, a kind of complex social economic system, the element of social sciences is requisite. As the Figure1 informs us, one critical parameter can be connected with another three or four ones, and mostly are determined by managers based on the relevantly internal and external factors, such as consumer loyalty, long term profits.

The VMI-APIOBPCS model was rebuilt by fuzzy difference equations, then genetic algorithms (GA) was adopted to search optimal parameters of fuzzy VMI-APIOBPCS model[9]. In final, bullwhip effect was reduced and the overall performance was bettered. Yohanes Kristianto cleverly inserted the fuzzy logic controller with dual-input and one-output into V-MI supply chain system, and lastly an ANOVA test, set to assess the assumptions, verified that the inventory response is effectively improved. This method can not only imitate the human thinking, but also absorbed managers' experience[14]. However, with the turbulent change of modern market and the management environment, the original experience may not be completely adaptable to the new surroundings.Fuzzy logic controller is kind of artificial intelligence and its implementation relies on complex computer techniques. As Filippo Neri said in [10], this kind of model can carry information about the volatility and the correlation among multi-factors, which enables the modern supply chain to be more flexible and accurate.

In view of above drawbacks and requirements, this paper inserts the fuzzy logic controller into the classic VMI-APIOBPCS model built in control engineering[6].But here the continuous-time version is considered. The potential fuzzy logic controller is connected with a more complex system than VMI with the expectation of extensive revenue. Then different weights are exerted on the dual fuzzy inputs further to enable the experience to suit the present surroundings.

The remaining parts of this paper proceeds as follows: section 2 includes the VMI-APIOBPCS model and introduces the related parameters should be fuzzy; introduces the complex fuzzy control theory and the fuzzy inference system applied in this paper and its optimization; the introduction of objection function. Section 3 shows us the simulation results and corre-



Figure 1: Causal loop diagram of VMI-APIOBPCS

sponding analysis. In section 4, the conclusions are made.

2 Fuzzy VMI-APIOBPCS Control Model

2.1 Construction of VMI-APIOBPCS Model

In 1961, Forrester firstly adopted industrial dynamics (equals to system dynamics) in the research of production and inventory control system. After that, Towill expanded the model into the form of IOBPC-S, moreover, carried out a string of optimizations of the system dynamic performance. Simon continuingly expanded the model into the more complex form of APIOBPCS with taking WIP into consideration[32]. And the VMI-APIOBPCS is the combination of VMI supply chain and APIOBPCS, which is displayed in Figure1, in which the variables are classified by different color: words colored green are control parameters in the system: words colored red are parameters been controlled; words colored blue are parameters based on observation or recording; words colored orange are the control parameters limited by consumer loyalty. Overall, the model of VMI-APIOBPCS synthesizes the multi-aspect interactions.

In VMI-APIOBPCS, distributors provide inventory information and data of sales to the supplier. Meanwhile, both of them reach a consensus in terms



Figure 2: Block diagram of VMI-APIOBPCS

of Reorder-point, in order to avoid excess inventory. While the inventory level of distributors below the Reorder-point, the supplier will supply the proper production automatically. Then, the manufacturer of the VMI supply chain will execute the function of APIOBPCS such that makes new production plan or distribution plan according to its inventory level.

Six parts are included in this system: 1) distributors' demand forecasting policy; 2) factory's demand forecasting policy; 3) the set of system inventory target; 5) the feedback loop of WIP; 6) production delay. We concluded them into two classes: demand forecasting policy and inventory policy. We can distinctly read the above knowledge in Figure 2(All the ins and outs in the above block diagram mean the connections with other subsystem that will be expressed in the following parts).

All in all, VMI-APIOBPCS, as an integrated management model, effectively slims down the supply chain system, smoothes the information and motivates the agile production.

2.1.1 Demand Forecasting Policy

We use exponential smoothing to predict the demand quantities of distributors and factory. For the sake of convenience, the sample time Δt is set for 1 in this continuous-time model.

According to [20], we can obtain the relationship between the factory's demand forecasting constant α_a and factory's time to average sales: $\alpha_a = 1/(1+Ta)$. For same argument, as to distributors, the relationship is: $\alpha_q = 1/(1+Tq)$. Forecast error ε is a stochastic variable, with mean zero. At last, the initial input of the whole system is consumer consumption such that market demand

$$CONS_t = \begin{cases} 0 & if \quad t < 0\\ 1 & if \quad t \ge 0 \end{cases}$$

2.1.2 Inventory Policy

In this paper, $TINV_t = 0[3, 6]$. Tp is a parameter beyond of control, restricted to manufacturing facility, product type, efficiency of production and so on[3], and in this paper we set Tp = 4. From the Figure2, we can obtain that the ORATE is decided by factory's demand forecasting, product of inventory deviation and (1/Ti), product of WIP deviation and (1/Tw). As to Ti, Tq is decided by α_i , α_a , such that $\alpha_i = 1/(1 + Ti)$, $\alpha_a = 1/(1 + Tw)[14]$. $T\bar{p}$ is the estimate of the average production delay, and $T\bar{p} = 4$. G is the proportion of distributors' safety stock between average consumption, reflecting the consumer service level.

2.1.3 Optimization of Parameters

Towill built the IOBPCS model, and acquired the optimal parameters by analyzing the sensitivity of the control parameters. Disney optimized the control variables (Ta, Ti, Tw, Tq, G, W) by simulation, and the results were assessed by ITAE (Product of Time and Absolute Error)[6]. Darya Kastsian adopted normal vector method to optimized the control parameter (Ta, Ti, Tw, Tq), based on the stability and robustness of system[33].

Kuo Ping Lin combined fuzzy mathematics and GA to obtain optimal dynamic performance of VMI-APIOBPCS [9]. Yohanes Kristianto pointed out there is a drawback for the forecast changed can unilaterally decided the smoothing constant. The decision support system should take more errors or inevitable deviations[14].

Disney obtained strict optimal parameters (Ta, Ti, Tw), based on the stability and robustness of system, then, analyzed the impact of change of single control parameter on the dynamic inventory response and received that the change of Ti incurred maximum variation of the dynamic inventory level[5]. To discern the indication of the fuzzy logic controller optimization more distinctly, we just choose Ti as our optimization parameter.

Furthermore, in order to make a more pragmatic optimization, we additionally select two deviations as the fuzzy inputs. According to [14], we select demand change and the difference between inventory level and demand as inputs.



Figure 3: Fuzzy logic controller

2.2 Complex Fuzzy Control Theory

The variables of complex system always have no definite relationships in mathematical sense, even are impossible to quantitative analysis with diverse assumptions[13, 15]. Traditional control theory is confined. In contrast, fuzzy control can make good use of experts' knowledge and experience, relying on fuzzy inference and decision-making to realize the control of complex system, especially the complex so-cial economic system with nonlinear lumped or distributed parameter [29, 30, 17].

The human factors in decision-making mainly include attitude to risk, intuition, experiences, or the combination of some of them. Those factors can directly act on the result of decision-making[1, 31]. In practical, managers can accumulate lot of experience that the management can receive excellent performance. If we can apply the experience in the future management, we can get good work.

In conclusion, fuzzy control can make good use of this experience, which can be an ideal method to investigate complex production-inventory issues.

2.2.1 Fuzzy Logic Controller

Fuzzy logic controller is the core of fuzzy control, including fuzzification input interface, fuzzy inference system (database, rule-base), defuzzification output interface.

1) Fuzzification input interface

Input variables should be fuzzified, then can be available to fuzzification input interface. As regards to fuzzification, we need to determine the fuzzy scale, which is inadvisable to be divided neither too raritas or too compact, otherwise, it is apt to induce bad consequence of information distortion. Besides, defuzzification should be in accordance with the membership function that is general in several forms such as straight lines, triangular, trapezoids, haversine, exponential[22]. And we adopt the simple and effective triangular one as our membership function,

Linguistic scale	input $\Delta(\delta, \varepsilon)$	Smoothing	
		$constant(\alpha)$	
Very High (VH)	$0.75 \leq \Delta \leq \infty$	0.5;1;1	
High (H)	$0.51{\leq}\Delta{\leq}0.74$	0.25;0.75;1	
Medium (M)	$0.26{\leq}\Delta{\leq}0.50$	0.25;0.5;0.75	
Low (L)	$0.05 \leq \Delta \leq 0.25$	0;0.25;0.75	
Very Low (VL)	$\Delta \leq 0.04$	0;0;0.5	

Table 1: Membership function



Figure 4: Membership function

which is expressed in Table1. We can understand it by Figure4 more intuitively.

In this paper, the two input variables are demand change (δ_t) and deviation between system level and demand (ε_t) . $\delta_t = D_t - D_{t-1}$, $\varepsilon_t = AINV_t - CONS_t$. ε_t can be produced by system itself in the simulation. Besides we assume $\delta_t = 0.2$ such that the demand change of system is 0.2 (Actually, the demand change is a stochastic variable, which is dependent on season, promotion, product life cycle and so on. Here we assume it as a constant just for simplifying simulation process).

2) Database

Database stores all the membership functions that are used in input and output, providing data to the inference system. In this paper, the membership functions of inputs and output are in form of Figure4, collaboratively.

Finally, the combination of database and rulebase produces the fuzzy inference system, which is illustrated by Figure5. After a series of fuzzy operations, all the rules can form the fuzzy rule curved surface, like Figure6.

In Figure 4 and Figure 6, ECa means smoothing constant α_i ; DEF means ε ; DC means δ .

3) Rule-base

The Rule-base of fuzzy logic controller is based on experts' knowledge and frontline workers' experience accumulated for long time, expressed as a lan-



Figure 5: Fuzzy inference system



Figure 6: Fuzzy rule camber

guage form of human intuitive inference. In general, we use 'If-then' as the rule that should be translated to enable the inference rule to be quantified. The rulebase of this paper is shown in Table2.

Finally, the combination of database and rulebase produces the fuzzy inference system, which is illustrated by Figure 5. After a series of fuzzy operations, all the rules can form the fuzzy rule curved surface, like Figure 6.

4) Defuzzification output interface

Defuzzification output interface can transform the fuzzy outputs into the normal form the control system can identify and accept. In this paper, we adopt the frequently-used centroid calculation, known as the center of gravity of area defuzzification (the explicit process, which is carried out in the fuzzy logic controller (FLC in Figure7, is in [14]). After defuzzification, we get the smoothing constant α_i , consequently converted though a series mathematical calculations into the form of Ti based on $\alpha_i = 1/(1 + Ti)$. The

			ε			
		VH	Н	Μ	L	VL
δ	VL	VL	VL	L	L	М
	L	VL	L	L	Μ	Н
	Μ	L	L	Μ	Н	Н
	Н	L	Μ	Н	Н	VH
	VH	М	Н	Н	VH	VH

Table 2: Rule-base

subsystem of the calculations in simulink is displayed in Figure7.

2.2.2 Optimization of Fuzzy Logic Controller

Generally, in the simple fuzzy logic controller, all inputs have the same influence on the fuzzy logic controller such that we rigidly follow the original experts' experience. However, this natural extraction of experts' a priori knowledge is not always easy or possible to realize[37], for some of the experience may not be suitable for present situation due to uncertainties. In this paper, after exerting different weights on the inputs by scaling factors, managers can flexibly master the inputs to be better for the control[24, 25, 26].

 μ , δ and ε are the fuzzy variable of their own discourse domain, so the control table of the simple fuzzy logic controller can be expressed by the following analysis formula.

$$\mu = \langle (\delta + \varepsilon) \div 2 \rangle \tag{1}$$

In order to enable the fuzzy logic controller to suit for different surroundings, we need to expand the control table to have more space to be revised. In this paper, we expand (1) into

$$\mu = \langle K1 \times \delta + K2 \times \varepsilon \rangle \tag{2}$$

 $K1, K2 \in (0,1)$. K1, K2 are independent from each other, used to regulate the degree of impact of inputs on fuzzy control. In other words, we consider the scaling factors K1, K2 as the subjective weights of inputs given by managers in different situations. Meantime, we assume $K1+K2 = 1, K1, K2 \in (0,1)$. Then we can adjust the scaling factors to find the optimal result.

2.3 Evaluation of Fuzzy VMI-APIOBPCS Control System

The complex of production-inventory system directly makes its evaluation intractable, for it is involved in versatile factors, such as dynamic response time, errors, deviations etc.. But in this paper, we have only one goal for evaluation of the system controlminimum cost. According to this criterion, we can draw up the objective function.

Towill evaluated the IOBPCS by

$$P.I. = \int_0^\infty ((COMRATE)^2 + \mu^2 (INV.DEV)^2) dt$$

, *COMRATE* means completion rate, INV.DEV means deviation between inventory and inventory tar-



Figure 7: Subsystem of transform calculations and scaling factors

get, μ means the weight coefficient[3]. Disney designed a comprehensive objective function

$$SCORE = \frac{1}{\sqrt{ITAE^2 + \omega_N^2 + PR^2 + WIPR^2 + SV^2}}$$

, ω_N is the noise of ORATE, meaning 'bullwhip effect' in management, PR means robustness to production lead-time variations, WIPR means robustness to pipeline level information fidelity, SV means systems selectivity), based on the stability and robustness for APIOBPCS [5]. Disney concisely adopted

$$SCORE = K \times VR_{ORATE} + VR_{AINV}$$

as the objective function of DE-APIOBPCS(a special situation of APIOBPCS, in which Ti equals to Tw).

Based on the deep thoughts about the features of VMI-APIOBPCS, we adopted three dimensions Euclidean distance as the form of objective function. The minimum value of the objective function is the best. The objective function is equation(3).

$$D = \sqrt{VR^2W + ITAE_{AINV}^2 + ITAE_{VCON}^2}$$
(3)
In (3),
$$VR = \left[\frac{\int_0^{t_s} (ORATE(t))^2 dt}{\int_0^{t_s} (CONS(t))^2 dt}\right]^2,$$
$$ITAE_{AINV} = \frac{\int_0^{t_s} |E_{AINV}| t dt}{a}, ITAE_{VCON} =$$

 $\frac{\int_0^{t_s} |E_{VCON}| tdt}{b}$ (t_s means the moment the system response becomes stable). In the following phase, the three parts of the objective will be interpreted explicitly.

1)
$$VR = \left[\frac{\int_0^{t_s} (ORATE(t))^2 dt}{\int_0^{t_s} (CONS(t))^2 dt}\right]^2$$

In this paper, VR is made to be the measurement of bullwhip effect, which is obviously different from the expression $\omega_N = \int_0^{\pi} |ORATE(\omega)|^2 d\omega$ in related works [3, 5].

In this paper, all the simulations are operated in time domain in which the tradition expression is refractory. Here, in order to gain precise data, we create a new form of metric for bullwhip effect strictly based on the definition of bullwhip effect (a tendency for small changes in end-consumer demand to be amplified as one moves further up the supply chain[8]. In communication engineering, $W' = \int_{-\infty}^{\infty} (f(t))^2 dt$ means the total power of signal (equals to the spectral density estimate). Naturally, $W' = \int_{0}^{t_0} (f(t))^2 dt$ (t_0 means particular moment) means the power of signal in a period of time. $O = \int_{0}^{t_s} (ORATE(t))^2 dt$ represents the total variations of order rate from the beginning of response to the last stability. The same argument, $I = \int_{0}^{t_s} (CONS(t))^2 dt$ represents for the total variations of consumer consumption from the beginning of response to the last stability. Then $VR = \left[\frac{\int_{0}^{t_s} (ORATE(t))^2 dt}{\int_{0}^{t_s} (CONS(t))^2 dt}\right]^2$ can be competent for the measurement of bullwhip effect. Its calculation subsystem is in the Figure8.

2)
$$ITAE_{AINV} = \frac{\int_0^{t_s} |E_{AINV}| t dt}{a},$$

 $ITAE_{VCON} = \frac{\int_0^{t_s} |E_{VCON}| t dt}{b}$

As to the meaning of $|E_{AINV}|$, $|E_{VCON}|$, we can refer to [6].

But the meaning of a, b is different. The function of a, b in $ITAE_{AINV}$, $ITAE_{VCON}$ is to simplify the value to the same order of magnitude. However, the coefficients inevitably change the proportion between



Figure 8: Subsystem of calculating VR



Figure 9: Subsystem of calculating ITAE

 $ITAE_{AINV}$ and $ITAE_{VCON}$ in the objective function. The subsystem of calculating ITAE in simulink is displayed in Figure 9.

When a = 250, the value of the subsystem is ITAE for inventory response, noted as ITAEainv; When a = 10, the value of the subsystem is ITAE for virtual demand, noted as ITAEvcon.

At last, the above three subsystems are assembled together to be the system of objective function, which is expressed in Figure 10.

3 Simulation Results and Analysis

In this paper, the simulation was implemented in the simulink of matlab7.0.1. The block diagram is shown in Figure 11.



Figure 10: Subsystem of objective function



Figure 12: Fine regulating function of scaling factors

We selected nine groups data of the control parameters in simulation and every group is simulated in the conditions with and without FLC. Besides, under the condition with FLC, the fuzzy input variables are given nine different weights (K1 = 0.9, K2 = 0.1; K1 = 0.8, K2 = 0.2; K1 = 0.7, K2 = 0.3; K1 = 0.6, K2 = 0.4; K1 = 0.5, K2 = 0.5; K1 = 0.4, K2 = 0.6; K1 = 0.3, K2 = 0.7; K1 = 0.2, K2 = 0.8; K1 = 0.1, K2 = 0.9). Take the simplicity of human thinking into consideration, we just choose the simple and intuitive numbers as the weights given to the fuzzy inputs.

3.1 Overall Dynamic Performance Comparison

In Table3, we can find that the values of objective function with FLC are obviously smaller than that without FLC. And after the regulation of scaling factors, the performance is further optimized. From Figure 13, the overall dynamic performances in the three different conditions are compared. The value of D without FLC is about three times larger than that with FLC. Figure 14 shows the effect of fine-tuning of the scaling factors on the performance of the whole system.

The distinct comparisons are the strongest evidence of optimizing quality. After the connection with fuzzy logic controller, the dynamic performance of VMI-APIOBPCS is greatly optimized. Although, the scaling factor cannot change the performance obviously, the fine-tuning can enable the managers to flexibly manipulate the business activities, so as to preserve the maximum profit in spite of disturbances.

3.2 Management Insights

In this paper, the fuzzy logic controller is applied to optimize the dynamic performance of VMI-

Value of control parameters	With FLC	Without FLC			
(Ta, Ti, Tq, Tw, G, W)	D	D(without Sf)	D(with Sf)	Optimal Sf	
(6, 7, 6, 42, 1, 1)	4.05	1.33	1.28	K1 = 0.9, K2 = 0.1	
(2, 16, 3, 35, 4, 0.2)	6.09	3.25	3.15	K1 = 0.9, K2 = 0.1	
(3, 3, 2, 4, 1, 0.05)	1.10	0.65	0.64	K1 = 0.9, K2 = 0.1	
(7, 12, 6, 63, 2, 5)	9.00	2.48	2.46	K1 = 0.9, K2 = 0.1	
(1, 5, 1, 5, 2, 0.01)	1.21	1.02	0.96	K1 = 0.9, K2 = 0.1	
(10, 20, 6, 63, 4, 20)	27.89	4.80	4.79	K1 = 0.6, K2 = 0.4	
(7, 27, 6, 63, 8, 5)	28.95	9.55	9.48	K1 = 0.7, K2 = 0.3	
(14, 27, 2, 63, 16, 1)	37.53	10.78	10.36	K1 = 0.4, K2 = 0.6	
(30, 26, 3, 35, 32, 1)	135.24	26.00	24.65	K1 = 0.8, K2 = 0.2	

 \diamondsuit Sf is the abbreviation of Scaling factor

 \diamond All the value of control parameters are recommended settings in[3].

 Table 3: Performance comparison



Figure 11: Block diagram of simulation



Figure 13: Overall dynamic performance



Figure 14: Comparison of inventory response



Figure 15: Comparison of ITAEainv



Figure 16: The ability to follow TINV

APIOBPCS model, furthermore, the fuzzy input variables are given different weights to adjust the knowledge in the new surroundings. After the investigation, we can reach the several important conclusions about innovations in this paper:

With the application human intelligence in the model, we can get new results that the fuzzy controller can greatly optimize the integrated performance of VMI-APIOBPCS. The scaling factors can tune the system performance finely, which makes the system optimization flexible to different new surroundings.

The dual-input, single input fuzzy logic controller can take demand and deviation between the inventory level and demand into consideration to make a more rational decision.

What's more, an auxiliary benefit, the inventory dynamic performance is largely improved. It is profitable for the inventory control.

After the conclusions, several points of management insight are obtained:

In the practice of forecasting, we should take more factors, both direct and indirect, into consideration according to the feature of our own business.

Production-inventory system is complex social economic system, in which human being play irreplaceable roles. Therefore, in the designing of optimization method, the unique thinking pattern needs to be taken into account.

In the process of management, we not only absorb the lessons but also conclude the precious experience. And we need to ponder how use the experience in the future work. This is the ideal of fuzzy control in this paper, meanwhile, the philosophy of learning organization[41].

When we adopt control engineering to research or optimize the production-inventory system, we should assess the practicability and whether it is proper for the control of production-inventory system, for it instinctively differently from the system like electronic and mechanical system[38, 39].

In a word, fuzzy control, as one kind of artificial intelligence, can imitate the way of human thinking, exploit experts' knowledge and experience, and renew the knowledge constantly. It is greatly significant to improve operational performance, reduce management cost, and elevate the flexibility[34, 40].

4 Conclusion

In this paper, the novel artificial intelligence–fuzzy control is adopted to optimize the productioninventory system. The simulation results verify that the overall dynamic performance is greatly improved and the inventory dynamic response is obviously improved. Fuzzy control can imitate thinking of human beings and make good use of experts' knowledge and experience to avoid the turbulent fluctuations in inventory dynamic changes.

By the way, further research can adopt optimization algorithm, liking GA, to initiatively search the optimal scaling factors, or investigate the effect of other variables on the determination of control parameters. Besides, the excellent inventory response may lay much pressure on the production, and this can be further researched. The relationship between the optimal performance and scaling factors can also be explored.

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References:

- [1] Muntean, M., Neri, F., Foreword to the special issue on collaborative systems, *WSEAS Transactions on Systems* 11,2012, pp. 617.
- [2] Bojkovic, Z., Neri, F., An introduction to the special issue on advances on interactive multimedia systems, *WSEAS Transactions on Systems* 12,2013, pp. 337–338.
- [3] D.R.Towill, Dynamics analysis of an inventory and order based production control system, *IN-T. J.PROD.RES* 6, 1982, pp. 671–687.
- [4] Azzouzi, M., Neri, F., An introduction to the special issue on advanced control of energy systems, WSEAS Transactions on Systems 8, 2013, pp. 103.
- [5] S.M.Disney, M.M.Naim, D.R.Towill, Genetic algorithm optimization of a class of inventory control systems, *Int. J. Production Economics* 68, 2000, pp. 259–278.
- [6] S.M Disney D.R.Towill, A procedure for the optimization of the dynamics response of a vendor managed inventory system, *Computors & Industrial Engineering* 43, 2002, pp. 27–58.
- [7] Haralambos Sarimveis, Panagiotis Patrinos, Chris D. Tarantilis, Chris T. Kiranoudis, Dynamic modeling and control of supply chain systems: A review, *Computers and Operations Research* 35, 2008, pp. 3530–3561.
- [8] Marko Jakšič, Borut Rusjan, The effect of replenishment policies on the bullwhip effect: A transfer function approach, *European Journal of Operational Research* 2007, pp. 1–16.

- [9] Kuo-Ping LinPing-Teng Chang, Kuo-Chen Hung, Ping-Feng Pai, A simulation of vendor managed inventory dynamics using fuzzy arithmetic operations with genetic algorithms, *Expert Systems with Applications* 10,2010, pp. 2571– 2579.
- [10] Neri, F., An introduction to the special issue on computational techniques for trading systems, time series forecasting, stock market modeling, financial assets modeling, *WSEAS Transactions on Systems* 11,2012, pp. 659–660.
- [11] Oğuz Solyalı, Haldun Süral, Haldun Sral, A single supplier-single retailer system with an order-up-to level inventory policy, *Operations Research Letters* 36,2008, pp. 543–546.
- [12] Joong Y. Son, Chwen Sheu, The impact of replenishment policy deviations in a decentralized supply chain, em Int. J. Production Economics 113, 2008, pp. 785–804.
- [13] Ciufudean, C., Neri, F, Open research issues on Multi-Models for Complex Technological Systems, WSEAS Transactions on Systems 13, 2014, in press.
- [14] Yohanes Kristianto, Petri Helo, Jianxin (Roger) Jiao, Maqsood Sandhu, Adaptive fuzzy vendor managed inventory control for mitigating the Bullwhip effect in supply chains, *European Journal of Operational Research* 216, 2012, pp. 346–355.
- [15] Neri, F., Open research issues on Computational Techniques for Financial Applications, *WSEAS Transactions on Systems* 13, 2014, in press.
- [16] White AS., Management of inventory using control theory, *International Journal of Technology Management* 17, 1999, pp. 847–60.
- [17] Doroshin, A. V., Neri, F., Open research issues on Nonlinear Dynamics, Dynamical Systems and Processes, *WSEAS Transactions on Systems* 13, 2014, in press.
- [18] B. Samanta, S.A. Al-Araimi, An inventory control model using fuzzy logic, *Int. J. Production Economics* 73, 2001, pp. 217–226.
- [19] Stephen M. Disney, Denis R. Towill, Roger D.H. Warburton, On the equivalence of control theoretic, differential, and difference equation approaches to modeling supply chains, *Int. J. Production Economics* 101, 2006, pp. 194–208.
- [20] Li Zhou, Mohamed M. Naim, Ou Tang, Denis R. Towill, Dynamic performance of a hybrid inventory system with a Kanban policy in remanufacturing process, *Omega* 34, 2006, pp. 585–598.

- [21] A. Ancarani, C. Di Mauro, D. D'Urso, A human experiment on inventory decisions under supply uncertainty, *Int. J. Production Economics* 142, 2013, pp. 61–73.
- [22] Swarup Medasani, Jaeseok Kim, Raghu Krishnapuram, An overview of membership function generation techniques for pattern recognition, *International Journal of Approximate Reasoning* 19, 1998, pp. 391-417.
- [23] Darya Kastsian, Martin Mönnigmann, Optimization of a vendor managed inventory supply chain with guaranteed stability and robustness*Int. J. Production Economics* 131, 2011, pp. 727–735.
- [24] Karthikeyan, P., Neri, F., Open research issues on Deregulated Electricity Market: Investigation and Solution Methodologies*WSEAS Transactions on Systems* 13, 2014, in press.
- [25] Panoiu, M., Neri, F., Open research issues on Modeling, Simulation and Optimization in Electrical SystemsWSEAS Transactions on Systems 13, 2014, in press.
- [26] Guarnaccia, C., Neri, F., An introduction to the special issue on recent methods on physical polluting agents and environment modeling and simulationWSEAS Transactions on Systems 12, 2013, pp. 53–54.
- [27] Carlsson, C., Fuller, R, A position paper on the agenda for soft decision analysis, *Fuzzy sets and systems* 131, 2002, pp. 3–11.
- [28] Wikner J, Naim MM, Towill DR. The system simplification approach in understanding the dynamic behaviour of a manufacturing supply chain, *Journal of Systems Engineering* 2, 1992, pp. 167–78.
- [29] Pekař, L., Neri, F., An introduction to the special issue on advanced control methods: Theory and application, WSEAS Transactions on Systems 12, 2013, pp. 301–303.
- [30] Neri, F., Open research issues on Advanced Control Methods: Theory and Application, *WSEAS Transactions on Systems* 13, 2014, in press.
- [31] David Collier, The human factors of project team decision-making for radioactive waste management, *Cogn Tech Work* 15,2013, pp. 47–58.
- [32] Simon J, Naim M.M, Towil D.RDynamic Analysis of a WIP Compensated I)ecision Support System, *International Journal of Manufactur*ing System Design 1,1994, pp. 283–297
- [33] J. Dejonckheere, S.M. Disney, M.R. Lambrecht, D.R. Towill, Measuring and avoiding the bullwhip effect: A control theoretic approach, *European Journal of Operational Research* 147, 2003, pp. 567–590.

- [34] Pekař, L., Neri, F., An introduction to the special issue on time delay systems: Modelling, identification, stability, control and applications, *WSEAS Transactions on Systems* 11,2012, pp. 539–540.
- [35] Chin-Teng Lin, Member, IEEE, Ya-Ching Lu, A Neural fuzzy system with fuzzy supervised learning, IEEE TRANSACTIONS ON SYSTEM-S, MAN, AND CYBERNETICS-PART B: CY-BERNETICS, 26, 1996.
- [36] Hamid R. Berenji, Member, IEEE, and Pratap Khedkar, *Learning and Tuning Fuzzy Logic Controllers Through Reinforcements*, IEEE TRANSACTIONS ON NEURAL NETWORKS 3, 1992.
- [37] Lionel Jouffe, Fuzzy Inference System Learning by Reinforcement Methods, IEEE TRANS-ACTIONS ON SYSTEMS, MAN, AND CYBERNETICS-PART C: APPLICATIONS AND REVIEWS, 28,1998.
- [38] Yohanes Kristianto, Angappa Gunasekaran, Petri Helo, Maqsood Sandhu, A decision support system for integrating manufacturing and product design into the reconfiguration of the supply chain networks, *Decision Support Systems* 52, 2012, pp. 790–801.
- [39] Kefeng Xu, Mark T. Leung, Stocking policy in a two-party vendor managed channel with space restrictions, *Int. J. Production Economics* 117, 2009, pp. 271–285.
- [40] Volos, C., Neri, F., An introduction to the special issue: Recent advances in defense systems: Applications, methodology, technology, WSEAS Transactions on Systems 11, 2012, pp. 477–478.
- [41] Hang bao Shang, Guo Shuang Tian, Cai Ping Song, Yun Kun Gao, Li Rong Chen, Xiang Hua Chen, Ying Li, The Study on the Relationship between Hypercompetition and Orgnizational Innovation: The Role of Organizational Learning, *Key Engineering Materials* 02, 2011, pp. 1236–1240.