Computation of Ancillary Service Requirement Assessment Indices for Load Frequency Control in a Restructured Power System using SMES unit

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Abstract: - This paper proposes various design procedures for computing Power System Ancillary Service Requirement Assessment Indices (PSASRAI) for a Two-Area Thermal Reheat Interconnected Power System (TATRIPS) in a restructured environment. In an interconnected power system, a sudden load perturbation in any area causes the deviation of frequencies of all the areas and also in the tie-line powers. This has to be corrected to ensure the generation and distribution of electric power companies to ensure good quality. The disturbances to the power system due to a small load change can even result in wide deviation in system frequency which is referred as Load-Frequency Control (LFC) problem. Quick system restoration is of prime importance not only based on the time of restoration and also stability limits also plays a very vital role in the power system operation even for the unexpected load variations in power systems. As the simple conventional Proportional plus Integral (P-I) controllers are still popular in power industry for frequency regulation as in case of any change in system operating conditions new gain values can be computed easily even for multi-area power systems, this paper focus on the computation of various PSASRAI for Two Area Thermal Reheat Interconnected Power System in restructured environment based on the settling time and peak over shoot concept of control input deviations of each area. Energy storage is an attractive option to augment demand side management implementation, so Superconducting Magnetic Energy Storage (SMES) unit can be efficiently utilized to meet the peak demand. So the design of the Proportional plus Integral (PI) controller gains for the restructured power system without and with SMES unit are carried out using Bacterial Foraging Optimization (BFO) algorithm. These controllers are implemented to achieve a faster restoration time in the output responses of the system when the system experiences with various step load perturbations. In this paper the PSASRAI are calculated for different types of possible transactions and the necessary remedial measures to be adopted are also suggested.


1 Introduction

Power system network comprises of several control areas and the various areas are interconnected through tie-lines. The scheduled energy exchange between control areas is enhanced through tie-lines. A small load fluctuation in any area causes the deviation of frequencies of all the areas and also of the tie-line power flow. These deviations have to be corrected through various supplementary controls. Maintaining frequency and power interchanges with interconnected control areas at the scheduled values are the major objectives of a Load Frequency Control (LFC) [1, 2]. The electric power business at present is largely in the hands of Vertically Integrated Utilities (VIU) which own generation, transmission and distribution systems that supply power to the customer at regulated rates. The electric power can be bought and sold between the interconnected VIU through the tie-lines and moreover such interconnection should provide greater reliability [1]. The major change that had happened is with the emergence of Independent Power Producers (IPP) which can sell power to VIU. In the restructure environment it is generally agreed that the first step is to separate the
generation of power from the transmission and distribution companies, thus putting all the generation on the same footing as the IPP [2]. In an interconnected power system, a sudden load perturbation in any area causes the deviation of frequencies of all the areas and also in the tie-line powers. This has to be corrected to ensure the generation and distribution of electric power companies to ensure good quality. This can be achieved by optimally tuning Load-Frequency controller gains. Many investigations in the area of Load-Frequency Control (LFC) problem for the interconnected power systems have been reported over the past six decades. A number of control strategies have been employed in the design of load-frequency controllers in order to achieve better dynamic performance [3-7]. The efficient incorporation of controllers will modify the transient response and steady state error of the system. Among the various types of load-frequency controllers, the most widely employed is the conventional Proportional plus Integral controller (PI). A lot of studies have been made related to LFC in a deregulated environment over last decades [8-12]. These studies try to modify the conventional LFC system to take into account the effect of bilateral contracts on the dynamics [3] and improve the dynamical transient response of the system [4-7] under various operating conditions. With the restructured electric utilities, the Load-Frequency Control requirements especially the nominal frequency in an interconnected power system besides maintaining the net interchange of power between control areas at predetermined values should be enhanced to ensure the quality of the power system. The importance of decentralized controllers for multi area load-frequency control in the restructured environment, where in, each area controller uses only the local states for feedback, is well known. The stabilization of frequency oscillations in an interconnected power system becomes challenging when implemented in the future competitive environment. So advanced economic, high efficiency and improved control schemes [12-14] are required to ensure the power system reliability for which Ancillary Services have to be adopted. Ancillary services can be defined as a set of activities undertaken by generators, consumers and network service providers and coordinated by the system operator that have to maintain the availability and quality of supply at levels sufficient to validate the assumption of commodity like behavior in the main commercial markets. There are different types of ancillary services such as voltage support, regulation, etc. The real power generating capacity related ancillary services, including Regulation Down Reserve (RDR), Regulation Up Reserve (RUR) in which regulation is the load following capability under Load Frequency Control (LFC) and spinning reserve (SR) is a type of operating reserve, which is a resource capacity synchronized to the system that is unloaded, is able to respond immediately to serve load, and is fully available within ten minutes but Non Spinning Reserve (NSR) are the one in which NSR is not synchronized to the system and Replacement Reserve (RR) is a resource capacity non synchronized to the system, which is able to serve load normally within thirty or sixty minutes. Reserves can be provided by generating units or interruptible load in some cases. Ancillary services can be divided into the following three categories and are listed below [15]. (i) Related to spot market implementation, short-term energy-balance and power system frequency. These will be labeled Frequency Control Ancillary Services (FCAS). (ii) Related to aspects of quality of supply other than frequency (primarily voltage magnitude and system security). These will be labeled Network Control Ancillary Services (NCAS). (iii) Related to system restoration or re-start following major blackouts. These will be labeled System Restoration Ancillary Services (SRAS).

In this paper various methodologies were adopted in computing Power System Ancillary Service Requirement Assessment Indices (PSASRAI) for Two-Area Thermal Reheat Interconnected Power System (TATRIPS) in a restructured environment. With the various Power System Ancillary Service Requirement Assessment Indices (PSASRAI) like Feasible Assessment Indices (FAI), Feasible Service Requirement Assessment Indices (FASRAI) Comprehensive Assessment Indices (CAI) or Comprehensive Service Requirement Assessment Indices (CASRAI) the remedial measures to be taken can be adjudged like integration of additional spinning reserve, incorporation of effective intelligent controllers, load shedding etc. In the early stages of power system restoration, the black start units are of the greatest interest because they will produce power for the auxiliaries of the thermal units without black start capabilities. Under this situation a conventional frequency control i.e., a governor may no longer be able to compensate for sudden load changes due to its slow response. Therefore, in an inter area mode, damping out the critical electromechanical oscillations is to be carried out effectively in the restructured power system. Moreover, the system’s control input
requirement should be monitored and remedial actions to overcome the control input deviation excursions are more likely to protect the system before it enters an emergency mode of operation. Special attention is therefore given to the behavior of network parameters, control equipments as they affect the voltage and frequency regulation during the restoration process which in turn reflects in PSASRAI. Now-a-days the complexities in the power system are being solved with the use of Evolutionary Computation (EC) such as Differential Evolution (DE) [16], Genetic Algorithms (GA), Practical Swarm Optimizations (PSO) [17] and Ant Colony Optimization (ACO) [18], which are some of the heuristic techniques having immense capability of determining global optimum. Classical approach based optimization for controller gains is a trial and error method and extremely time consuming when several parameters have to be optimized simultaneously and provides suboptimal result. Some authors have applied GA to optimize the controller gains more efficiently, but the premature convergence of GA degrades its search capability [19]. Recent research has brought out some deficiencies in using GA, PSO based techniques [20- 21]. The Bacterial Foraging Optimization [BFO] mimics how bacteria forage over a landscape of nutrients to perform parallel non gradient optimization [22]. The BFO algorithm is a computational intelligence based technique that is not affected larger by the size and nonlinearity of the problem and can be convergence to the optimal solution in many problems where most analytical methods fail to converge. This more recent and powerful evolutionary computational technique BFO [23-24] is found to be user friendly and is adopted for simultaneous optimization of several parameters for both primary and secondary control loops of the governor. Most options proposed so far for LFC have not been implemented due to system operational constraints associated with thermal power plants. The main reason is the non-availability of required power other than the stored energy in the generator rotors, which can improve the performance of the system, in the wake of sudden increased load demands. A fast acting Superconducting Magnetic Energy Storage unit (SMES) can effectively damp the electromechanical oscillations occurring in the power system, because they provide storage capacity in addition to the kinetic energy of the generator rotor which can share the sudden changes. In this study, BFO algorithm is used to optimize the Proportional plus Integral (PI) controller gains for the load frequency control of a Two-Area Thermal Reheat Interconnected Power System (TATRIPS) in a restructured environment with and without SMES unit. Various case studies are analyzed to develop Power System Ancillary Service Requirement Assessment Indices (PSASRAI) namely, Feasible Assessment Index (FAI) and Complete Assessment Index (CAI) which are able to predict the normal operating mode, emergency mode and restorative modes of the power system.

2 Modelling of a Two-Area Thermal Reheat interconnected Power system (TATRIPS) in restructured scenario

Fig.1. Schematic diagram of two-area system in restructured environment

In the restructured competitive environment of power system, the Vertically Integrated Utility (VIU) no longer exists. The deregulated power system consists of GENCOs, DISCOs, and Transmissions Companies (TRANSCOs) and Independent System Operator (ISO). GENCOs which will compete in a free market to sell the electricity they produce. Mostly the retail customer will continue for some time to buy from the local distribution company and distribution companies have been designated as DISCOs. The entities that will wheel this power between GENCOs and DISCOs have been designated as TRANSCOs. Although it is conceptually clean to have separate functionalities for the GENCOs, TRANSCOs and DISCOs, in reality there will exist companies with combined or partial responsibilities. With the emergence of the distinct identities of GENCOs, TRANSCOs, DISCOs and the ISO, many of the ancillary services of a VIU will have a different role to play and hence have to be modeled differently. Among these ancillary service controls one of the most important services to be enhanced is the Load-frequency control [18]. The LFC in a deregulated electricity market should be designed to consider different types of possible transactions, such as poolco-based transactions, bilateral transactions and a combination of these two [19, 20]. In the new scenario, a DISCO can contract individually with a GENCO for acquiring the power and these transactions will be made under the supervision of
ISO. To make the visualization of contracts easier, the concept of “DISCO Participation Matrix” (DPM) is used which essentially provides the information about the participation of a DISCO in contract with a GENCO. In DPM, the number of rows has to be equal to the number of GENCOs and the number of columns has to be equal to the number of DISCOs in the system. Any entry of this matrix is a fraction of total load power contracted by a DISCO toward a GENCO. As a result, the total of entries of column belong to DISCOi of DPM is 1 = \sum_{j=1}^{N} pf_{ij}. In this study two-area interconnected power system in which each area has two GENCOs and two DISCOs. Let GENCO 1, GENCO 2, DISCO 1, DISCO 2 be in area 1 and GENCO 3, GENCO 4, DISCO 3, DISCO 4 be in area 2 as shown in Fig 1. The corresponding DPM is given as follows [1-4]

\[
DPM = \begin{bmatrix}
  D & I & S & C & O \\
  cpf_{11} & cpf_{12} & cpf_{13} & cpf_{14} & \\
  cpf_{21} & cpf_{22} & cpf_{23} & cpf_{24} & \\
  cpf_{31} & cpf_{32} & cpf_{33} & cpf_{34} & \\
  cpf_{41} & cpf_{42} & cpf_{43} & cpf_{44}
\end{bmatrix}
\]

Where \( cpf \) represents “Contract Participation Factor” and is like signals that carry information as to which the GENCO has to follow the load demanded by the DISCO. The actual and scheduled steady state power flow through the tie-line are given as

\[
\Delta P_{\text{tie}-2, \text{scheduled}} = \sum_{i=1}^{4} \sum_{j=3}^{4} cpf_{ij} \Delta P_{Lj} = \sum_{j=1}^{4} \sum_{i=3}^{4} cpf_{ij} \Delta P_{Lj}
\]

\[
\Delta P_{\text{tie}-2, \text{actual}} = (2 \pi T_{12} / s) (\Delta F_{1} - \Delta F_{2})
\]

And at any given time, the tie-line power error \( \Delta P_{\text{tie}-2, \text{error}} \) is defined as

\[
\Delta P_{\text{tie}-2, \text{error}} = \Delta P_{\text{tie}-2, \text{actual}} - \Delta P_{\text{tie}-2, \text{scheduled}}
\]

The error signal is used to generate the respective ACE signals as in the traditional scenario [6]

\[
ACE_{1} = \beta_{1} \Delta F_{1} + \Delta P_{\text{tie}-1-2, \text{error}}
\]

\[
ACE_{2} = \beta_{2} \Delta F_{2} + \Delta P_{\text{tie}-2-1, \text{error}}
\]

For two area system as shown in Fig.1, the contracted power supplied by \( i \)th GENCO is given as

\[
\Delta P_{L, \text{actual}} = \sum_{j=1}^{4} cpf_{ij} \Delta P_{Lj}
\]

Also note that \( \Delta P_{L1, \text{LOC}} = \Delta P_{L1} + \Delta P_{L2} \) and \( \Delta P_{L2, \text{LOC}} = \Delta P_{L3} + \Delta P_{L4} \). In the proposed LFC implementation, contracted load is fed forward through the DPM matrix to GENCO set points. The actual loads affect system dynamics via the input \( \Delta P_{L, \text{LOC}} \) to the power system blocks. Any mismatch between actual and contracted demands will result in frequency deviations that will drive LFC to re dispatch the GENCOs according to ACE participation factors, i.e., \( apf_{11}, apf_{12}, apf_{21} \) and \( apf_{22} \). The state space representation of the minimum realization model of ‘\( N \)’ area interconnected power system may be expressed as [14].

\[
\begin{align*}
\dot{x} &= Ax + Bu + \Gamma d \\
y &= Cx
\end{align*}
\]

Where

\[
x = [x_{1}^T, \Delta p_{e1}, \ldots , x_{N-1}^T, \Delta p_{e(N-1)}, \ldots , x_{N}^T]^T
\]

\( u = [u_{1}, \ldots , u_{N}]^T = [\Delta P_{C1}, \ldots , \Delta P_{CN}]^T \)

\( n = \sum_{i=1}^{N} n_{i} + (N - 1) \)

\( d = [d_{1}, \ldots , d_{N}]^T = [\Delta P_{D1}, \ldots , \Delta P_{DN}]^T \)

\( y = [y_{1}, \ldots , y_{N}]^T, 2N \) - Measurable output vector

\[
A = \begin{bmatrix}
  \Delta F_{1} \\
  \Delta F_{2} \\
  \Delta F_{3} \\
  \Delta F_{4} \\
  \Delta F_{S}
\end{bmatrix}, E
\]

\[
C = \begin{bmatrix}
  \Delta P_{L1} \\
  \Delta P_{L2} \\
  \Delta P_{L3} \\
  \Delta P_{L4} \\
  \Delta P_{S}
\end{bmatrix}
\]

\[
\begin{bmatrix}
  \Delta F_{S} \\
  \Delta P_{S}
\end{bmatrix}
\]

\( \Gamma \) is the disturbance distribution matrix, \( C \) is the control output distribution matrix, \( x \) is the state vector, \( u \) is the control vector and \( d \) is the disturbance vector consisting of load changes.

### 3 Modeling of Superconducting Magnetic Energy Storage unit (SMES)

Generally the application of energy storages to electrical power system can be grouped into two categories i.e. Storage meant for load leveling application and to improve the dynamic performance of power system. SMES have the following advantages like the time delay during charge and discharging is quite short, Capability of controlling both active and reactive power simultaneously, Loss of power is less, High...
reliability, High efficiency. Moreover, SMES stabilizes the frequency oscillations by absorbing/injecting the active power. Fig 2 shows the block diagram representation of the SMES unit. To achieve quick restoration of the current, the inductor current deviation can be sensed and used as a negative feedback signal in the SMES control loop [25]. In a two-area interconnected thermal restructured power system under with the sudden small disturbances which continuously disturb the normal operation of power system. As a result the requirement of frequency controls of areas beyond the governor capabilities SMES is located in area1 absorbs and supply required power to compensate the load fluctuations. Tie-line power flow monitoring is also required in order to avoid the blackout of the power system. The normal operation of a power system is continuously disturbed due to sudden small load perturbations. The problem lies in the fact that the inertia of the rotating parts is the only energy storage capacity in a power system. Thus, when the load-end of the transmission line experiences small load changes, the generators need continuous control to suppress undesirable oscillations in the control to suppress undesirable oscillations in the system. The SMES is a fast acting device which can swallow these oscillations and help in reducing the frequency and tie-line Power deviations for better performance of system disturbances. A SMES which is capable of controlling active and reactive power simultaneously has been expected as one if the most effective stabilizers for power oscillations [26- 29]. Besides oscillation control, a SMES allows a load leveling, a power quality improvement and frequency stabilization. A typical SMES system includes three parts namely superconducting coil, power conditioning system and cooled refrigerator. From the practical point of view, a SMES unit with small storage capacity can be applied not only as a fast compensation device for power consumptions of large loads, but also as a robust stabilizer for frequency oscillations.

The schematic diagram in Fig 3 shows the configuration of a thyristor controlled SMES unit. The SMES unit contains DC superconducting Coil and converter which is connected by Y–D/Y–Y transformer. The inductor is initially charged to its rated current I_{do} by applying a small positive voltage. Once the current reaches the rated value, it is maintained constant by reducing the voltage across the inductor to zero since the coil is superconducting. Neglecting the transformer and the converter losses, the DC voltage is given by

$$E_d = 2V_{do} \cos \alpha - 2I_d R_c.$$  \hspace{1cm} (9)$$

Where $E_d$ is DC voltage applied to the inductor, firing angle ($\alpha$), $I_d$ is current flowing through the inductor. $R_c$ is equivalent commutating resistance and $V_{do}$ is maximum circuit bridge voltage. Charge and discharge of SMES unit are controlled through change of commutation angle $\alpha$. In LFC operation, the dc voltage $E_d$ across the superconducting inductor is continuously controlled depending on the sensed Area Control Error (ACE) signal. Moreover, the inductor current deviation is used as a negative feedback signal in the SMES control loop. So, the current variable of SMES unit is intended to be settling to its steady state value. If the load is used as a negative feedback signal in the SMES control demand changes suddenly, the feedback provides the prompt restoration of current. The inductor current must be restored to its nominal value quickly after a system disturbance, so that it can respond to the next load disturbance immediately. As a result, the energy stored at any instant is given by

$$W_{sm}(\tau) = W_{sm}(0) + \int_{\tau_0}^{\tau} P_{sm}(\tau)d\tau$$  \hspace{1cm} (10)$$

Where, $W_{sm}(\tau) = \frac{1}{2} L I^2$, initial energy in the inductor. Equations of inductor voltage deviation and current deviation for each area in Laplace domain are as follows

$$\Delta E_d(s) = \frac{K_{SMES}}{1+Ts} \left[ \beta \Delta P_{l}(s) + \Delta P_{w}(s) \right] - \frac{K_{id}}{1+Ts} \Delta I_{d}(s)$$ \hspace{1cm} (11)$$

$$\Delta I_{d}(s) = (1/TL_{d}) \Delta E_d(s)$$ \hspace{1cm} (12)$$

Where, $\Delta E_d(s) = \text{converter voltage deviation applied to inductor in SMES unit}$

$K_{SMES} = \text{Gain of the control loop SMES}$

$T_{dci} = \text{converter time constant in SMES unit}$

$K_{id} = \text{gain for feedback}$

$\Delta I_{d}(s) = \text{inductor current deviation in SMES unit}$

The deviation in the inductor real power of SMES unit is expressed in time domain as follows [30].

$$\Delta P_{SMES}(t) = \Delta E_{d} I_{dci} + \Delta I_{d} \Delta E_{d}$$ \hspace{1cm} (13)$$

The Linerized model of a two-area thermal reheat interconnected power system in restructured environment with SMES unit shown in Fig.4.
4 Design of decentralized PI controllers

The proportional plus integral controller gain values \((K_p, K_i)\) are tuned based on the settling time of the output response of the system (especially the frequency deviation) using Bacterial Foraging Optimization (BFO) technique. The closed loop stability of the system with decentralized PI controllers are assessed using settling time of the system output response \([31]\). It is observed that the system whose output response settles fast will have minimum settling time based criterion \([32]\) and can be expressed as

\[
F(K_p, K_i) = \min (\zeta_i)
\]

\[
U_1 = -K_p \int ACE_1 - K_i \int ACE_1 \, dt,
\]

\[
U_2 = -K_p \int ACE_2 - K_i \int ACE_2 \, dt
\]

Where,

\(K_p\) = Proportional gain

\(K_i\) = Integral gain

\(ACE\) = Area Control Error

\(U_1, U_2\) = Control input requirement of the respective areas.

\(\zeta_i\) = settling time of the frequency deviation of the \(i^{th}\) area under disturbance

The relative simplicity of this controller is a successful approach towards the zero steady state error in the frequency of the system. With these optimized gain values the performance of the system is analyzed and various PSRAI are computed.

5 Bacterial Foraging Optimization (BFO) Technique

**Review of Bacterial Foraging Optimization**

The BFO method was introduced by Possino \([21]\) motivated by the natural selection which tends to eliminate the animals with poor foraging strategies and favour those having successful foraging strategies. The foraging strategy is governed by four
processes namely Chemotaxis, Swarming, Reproduction and Elimination and Dispersal. Chemotaxis process is the characteristics of movement of bacteria in search of food and consists of two processes namely swimming and tumbling. A bacterium is said to be swimming if it moves in a predefined direction, and tumbling if it starts moving in an altogether different direction. To represent a tumble, a unit length random direction \( \phi(j) \) is generated. Let, “\( j \)” is the index of chemotactic step, “\( k \)” is reproduction step and “\( l \)” is the elimination dispersal event. \( \theta(j,k,l) \), is the position of \( j^{th} \) bacteria at \( j^{th} \) chemotactic step \( k^{th} \) reproduction step and \( l^{th} \) elimination dispersal event. The position of the bacteria in the next chemotactic step after a tumble is given by

\[
\theta'((j+1), k, l) = \theta'(j, k, l) + C(i) \phi(j)
\]

If the health of the bacteria improves after the tumble, the bacteria will continue to swim to the same direction for the specified steps or until the health degrades. Bacteria exhibits swarm behavior i.e. healthy bacteria try to attract other bacterium so that together they reach the desired location (solution point) more rapidly. The effect of swarming [22] is to make the bacteria congregate into groups and moves as concentric patterns with high bacterial density. Mathematically swarming behavior can be modeled

\[
\begin{align*}
J_{cc}(\theta, p(j,k,l)) &= \sum_{i=1}^{S} J_{cc}(\theta(j,k,l)) \\
&= \sum_{i=1}^{S} -d_{attract} \exp(-\omega_{attract} \sum_{n=1}^{p} (\phi_{n} - \phi_{i})^{2}) \\
&+ \sum_{i=1}^{S} -h_{repellent} \exp(-\omega_{repellent} \sum_{n=1}^{p} (\phi_{n} - \phi_{i})^{2})
\end{align*}
\]

Where

\( J_{cc} \) - Relative distance of each bacterium from the fittest bacterium
\( S \) - Number of bacteria
\( p \) - Number of parameters to be optimized
\( \theta^{m} \) - Position of the fittest bacteria
\( d_{attract}, \omega_{attract}, h_{repellent}, \omega_{repellent} \) different coefficients representing the swarming behavior of the bacteria which are to be chosen properly.

In Reproduction step, population members who have sufficient nutrients will reproduce and the least healthy bacteria will die. The healthier population replaces unhealthy bacteria which get eliminated owing to their poorer foraging abilities. This makes the population of bacteria constant in the evolution process. In this process a sudden unforeseen event may drastically alter the evolution and may cause the elimination and / or dispersion to a new environment. Elimination and dispersal helps in reducing the behavior of stagnation i.e., being trapped in a premature solution point or local optima.

### Bacterial Foraging Algorithm

In case of BFO technique each bacterium is assigned with a set of variable to be optimized and are assigned with random values \([ A ]\) within the universe of discourse defined through upper and lower limits between which the optimum value is likely to fall. In the proposed method of proportional plus integral gain \((K_{ps}, K_{i}) (i = 1, 2)\) scheduling, each bacterium is allowed to take all possible values within the range and the cost objective function which is represented by Eq (16) is minimized. In this study, the BFO algorithm reported in [22] is found to have better convergence characteristics and is implemented as follows.

1. **Initialization**;
2. **Number of parameter** \((p)\) to be optimized.
3. **Number of bacterial** \((S)\) to be used for searching the total region.
4. **Swimming length** \((N_{s})\), after which tumbling of bacteria will be undertaken in a chemotactic loop.
5. **NC** - the number of iteration to be undertaken in a chemotactic loop \((NC>N_{S})\)
6. **Np** - the maximum number of reproduction to be undertaken.
7. **N_ed** - the maximum number of elimination and dispersal events to be imposed over bacteria
8. **Pr** - the probability with which the elimination and dispersal events will continue.
9. **Location of each bacterium** \(P(l-p, l-s, l)\) which is specified by random numbers within \([-1, 1]\)
10. The value of \(C(i)\), which is assumed to be constant in this case for all bacteria to simplify the design strategy.
11. The value of \(d_{attract}, W_{attract}, h_{repellent}\) and \(W_{repellent}\) must be same so that the penalty imposed on the cost function through “\(J_{cc}\)”, of Eq (16) will be “0” when all the bacteria will have same value, i.e. they have converged. After initialization of all the above variables, keeping one variable changing and others fixed the value of “U” is obtained by obtaining the simulation of system using the parameter contained in each bacterium. For the corresponding minimum cost, the magnitude of the changing variable is selected. Similar procedure is carried out for other variables keeping the already optimized one unchanged. In this way all the
variables of step 1- initialization are obtain and are presented below. \( S = 6, N_c = 10, N_s = 3, N_{re} = 15, N_{ed} = 2, P_{ed} = 0.25, d_{attract} = 0.01, w_{attract} = 0.04, h_{repelent} = 0.01, \) and \( w_{repelent} = 10, \) \( p = 2. \)

Step - 2 Iterative algorithms for optimization:

This section models the bacterial population chemotaxis Swarming, reproduction, elimination, and dispersal (initially, \( j = k = l = 0 \)) for the algorithm updating \( \theta' \) automatically results in updating of \( P' \).

1. Elimination –dispersal loop: \( l = l + 1 \)
2. Reproduction loop: \( k = k + 1 \)
3. Chemotaxis loop: \( j = j + 1 \)
   a) For \( i = 1, 2, \ldots S \), calculate cost for each bacterium \( i \) as follows.
   
   Compute value of cost \( J(i, j, k, l) \)

   
   Let

   \[ J_{sw}(i, j, k, l) = J(i, j, k, l) + J_{ec}(\theta'(j, k, l), P(j, k, l)) \]

   
   [i.e., add on the cell to cell attractant effect obtained through Eq (16) for swarming behavior to obtain the cost value obtained through Eq (14)].

   Let \( J_{last} = J_{sw}(i, j, k, l) \) to save this value since a better cost via a run be found.

   End of for loop.

   b) for \( i = 1, 2, \ldots S \) take the tumbling / swimming decision.

   Tumble: generate a random vector \( \Delta(i) \in \mathbb{R}^p \) with each element \( \Delta_m(i) \) \( m = 1, 2, \ldots, p \), a random number ranges from \([-1, 1]\).

   Move the position the bacteria in the next chemotactic step after a tumble by Eq (15). Fixed step size in the direction of tumble for bacterium \( i \) is considered

   Compute \( J(i, j + 1, k, l) \) and then let

   \[ J_{sw}(i, j + 1, k, l) = J(i, j + 1, k, l) + J_{ec}(\theta'(j + 1, k, l), P(j + 1, k, l)) \]

   \[ J_{sw}(i, j + 1, k, l) \quad (17) \]

   Swim:

   Let \( m = 0 \) (counter for swim length)

   While \( m < N_{sw} \) (have not climbed down too long)

   Let \( m = m + 1 \)

   If \( J_{sw}(i, j + 1, k, l) < J_{last} \) (if doing better), let

   \[ \theta'(j + 1, k, l) = \theta'(j, k, l) + C(i) \frac{\Delta(i)}{\sqrt{\Delta(i) \cdot \Delta(i)}} \quad (18) \]

   Where \( C(i) \) denotes step size; \( \Delta(i) \) Random vector; \( \Delta'(i) \) Transpose of vector \( \Delta(i) \).

   The new \( J(i, j + 1, k, l) \) is computed. Else let \( m = N_s \). This the end of while statement

   c) Go to next bacterium \( i + 1 \) is selected if \( i \neq S \) (i.e. go to step- b) to process the next bacterium

4. If \( j < N_c \) go to step 3. In this case, chemotaxis is continued since the life of the bacteria is not over.

5. Reproduction

   a) For the given \( k \) and \( l \) for each \( i = 1, 2, \ldots \), let

   \[ J_{health} = \min _{j = 1, 2, \ldots S} \{ J_{sw}(i, j, k, l) \} \]

   be the health of the bacterium \( i \) (a measure of how many nutrients it got over its life time and how successful it was in avoiding noxious substance). Sort bacteria in the order of ascending cost \( J_{health} \) (higher cost means lower health).

   b) when \( S_r = S/2 \) bacteria with highest \( J_{health} \) values die and other \( S_r \) bacteria with the best Value split [and the copies that are placed at the same location as their parent].

6. If \( k < N_{re} \) go to 2; in this case, as the number of specified reproduction steps have not been reached, so the next generation in the chemotactic loop is to be started.

7. Elimination –dispersal: for \( i = 1, 2, \ldots S \) with probability \( P_{ed} \), eliminates and disperses each bacterium [this keeps the number of bacteria in the population constant] to a random location on the optimization domain.

6 Simulation Results and Observations

The Two-Area Thermal Reheat Interconnected Restructured Power System considered for the study consists of two GENCOs and two DISCOs in each area. The nominal parameters are given in Appendix. The optimal solution of control inputs is taken an optimization problem, and the objective function (14) is obtained using the frequency deviations of control areas and tie-line power changes. The Proportional plus Integral controller gains \((K_p, K_i)\) are tuned with BFO algorithm by optimizing the solutions of control inputs for the various case studies as shown in Table 1.

The results are obtained by MATLAB 7.0.1 software and 100 iterations are chosen for the convergence of the solution in the BFO algorithm. These PI controllers are implemented in a Two-Area Thermal Reheat Interconnected restructured Power System with SMES unit considering different utilization of capacity \((K=0, 0.25, 0.5, 0.75, 1.0)\) and for different type of transactions. The corresponding frequency deviations \( \Delta f \), tie-line power deviation \( \Delta P_{tie} \) and control input deviations \( \Delta P_c \) are obtained with respect to time.
as shown in Fig 5-6. Simulation results reveal that the proposed PI controller for LFC system and coordinated with SMES units greatly reduces the peak over shoot / under shoot of the frequency deviations and tie-line power flow deviation. And also it reduces the control input requirements and the settling time of the output responses also reduced considerably is shown in Table 3. More over Power System Ancillary Service Requirement Assessment Indices (PSASRAI) namely, Feasible Assessment Indices (FAI) when the system is operating in a normal condition with both units in operation and Comprehensive Assessment Indices (CAI) are one or more unit outage in any area are obtained as discussed. In this study GENCO-4 in area 2 is outage are considered. From these Assessment Indices indicates the restorative measures like the magnitude of control input requirement, rate of change of control input requirement can be adjudged.

**Feasible Restoration Indices**

### 6.1 Scenario 1: Poolco based transaction

The optimal Proportional plus Integral (PI) controller gains are obtained for TATRIPS considering various case studies for framing the Feasible Assessment Indices (FAI) which were obtained based on Area Control Error (ACE) as follows:

**Case 1:** In the TATRIPS considering both areas have two thermal reheat units. Consider a case where the GENCOs in each area participate equally in LFC. For Poolco based transaction: the load change occurs only in area 1. It denotes that the load is demanded only by DISCO 1 and DISCO 2. Let the value of this load demand be 0.1 p.u MW for each of them i.e. \( \Delta P_{L1} = 0.1 \) p.u MW, \( \Delta P_{L2} = 0.1 \) p.u MW, \( \Delta P_{L3} = \Delta P_{L4} = 0.0 \). DISCO Participation Matrix (DPM) referring to Eq (1) is considered as [1-4]

\[
DPM = \begin{bmatrix}
0.5 & 0.5 & 0 & 0 \\
0.5 & 0.5 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 
\end{bmatrix}
\] (19)

Note that DISCO 3 and DISCO 4 do not demand power from any GENCOs and hence the corresponding contract participation factors (columns 3 and 4) are zero. DISCO 1 and DISCO 2 demand identically from their local GENCOs, viz., GENCO 1 and GENCO 2. Therefore, \( cpf_{11} = cpf_{12} = 0.5 \) and \( cpf_{21} = cpf_{22} = 0.5 \). The frequency deviations (\( \Delta F \)) of areas, tie-line power deviation (\( \Delta P_{tie} \)) and control input requirements deviations (\( \Delta P_c \)) of both areas are as shown the Fig 5. The settling time (\( \varsigma_{1} \)) and peak over /under shoot (\( Mp_{p} \)) of the control input deviations (\( \Delta P_{c} \)) in both the area were obtained from Fig 5 (d) and (e). From the Fig 5 (d) and (e) the corresponding Feasible Assessment Indices \( FAI_1, FAI_2, FAI_3 \) and \( FAI_4 \) are calculated as follows:

**Step 6.1** The Feasible Assessment Index 1 (\( \varepsilon_1 \)) is obtained from the ratio between the settling time of the control input deviation \( \Delta P_{c1} (\varsigma_{1}) \) response of area 1 and power system time constant (\( T_{p1} \)) of area 1

\[
FRI_1 = \frac{\Delta P_{c1} (\varsigma_{1})}{T_{p1}}
\] (20)

**Step 6.2** The Feasible Assessment Index 2 (\( \varepsilon_2 \)) is obtained from the ratio between the settling time of the control input deviation \( \Delta P_{c2} (\varsigma_{2}) \) response of area 2 and power system time constant (\( T_{p2} \)) of area 2

\[
FRI_2 = \frac{\Delta P_{c2} (\varsigma_{2})}{T_{p2}}
\] (21)

**Step 6.3** The Feasible Assessment Index 3 (\( \varepsilon_3 \)) is obtained from the peak value of the control input deviation \( \Delta P_{c1} (\varsigma_{3}) \) response of area 1 with respect to the final value \( \Delta P_{c1} (\varsigma_{4}) \)

\[
FRI_3 = \Delta P_{c1} (\varsigma_{3}) - \Delta P_{c1} (\varsigma_{4})
\] (22)

**Step 6.4** The Feasible Assessment Index 4 (\( \varepsilon_4 \)) is obtained from the peak value of the control input deviation \( \Delta P_{c2} (\varsigma_{p}) \) response of area 1 with respect to the final value \( \Delta P_{c2} (\varsigma_{s}) \)

\[
FRI_4 = \Delta P_{c2} (\varsigma_{p}) - \Delta P_{c2} (\varsigma_{s})
\] (23)

**Case 2:** This case is also referred a Poolco based transaction on TATRIPS where in the GENCOs in each area participate not equally in LFC and load demand is more than the GENCO in area 1 and the load demand change occurs only in area 1. This condition is indicated in the column entries of the DPM matrix and sum of the column entries is more than unity.

**Case 3:** It may happen that a DISCO violates a contract by demanding more power than that specified in the contract and this excess power is not contracted to any of the GENCOs. This uncontracted power must be supplied by the GENCOs in the same area to the DISCO. It is
represented as a local load of the area but not as the contract demand. Consider scenario-1 again with a modification that DISCO 1 demands 0.1 p.u MW of excess power i.e., ∆Puc_1 = 0.1 p.u MW and ∆Puc_2 = 0.0 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = ∆P_{uc1} + ∆P_{uc2} = 0.1 + 0.0 = 0.1 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = ∆P_{uc1} + ∆P_{uc2} = 0.1 + 0.0 = 0.1 p.u MW.

Case 4: This case is similar to Case 2 to with a modification that DISCO 3 demands 0.1 p.u MW of excess power i.e., ∆Puc_3 = 0.1 p.u MW and ∆Puc_4 = 0.05 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 + Load of DISCO 3 = ∆P_{uc1} + ∆P_{uc2} + ∆P_{uc3} = 0.1 + 0.0 + 0.1 = 0.2 p.u MW.

Case 5: In this case which is similar to Case 2 with a modification that DISCO 3 demands 0.15 p.u MW of excess power i.e., ∆Puc_3 = 0.15 p.u MW and ∆Puc_4 = 0.05 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 + Load of DISCO 3 + Load of DISCO 4 = ∆P_{uc1} + ∆P_{uc2} + ∆P_{uc3} + ∆P_{uc4} = 0.1 + 0.0 + 0.1 + 0.15 = 0.3 p.u MW.

Case 6: Here all the DISCOs have contract with the GENCOs and the following DISCO Participation Matrix (DPM) be considered [1-4].

\[
DPM = \begin{bmatrix}
0.4 & 0.25 & 0.2 & 0.4 \\
0.3 & 0.15 & 0.1 & 0.2 \\
0.1 & 0.4 & 0.3 & 0.25 \\
0.2 & 0.2 & 0.4 & 0.15
\end{bmatrix}
\]

(24)

In this case, the DISCO 1, DISCO 2, DISCO 3 and DISCO 4, demands 0.15 p.u MW, 0.05 p.u MW, 0.15 p.u MW and 0.05 p.u MW from GENCOs as defined by cpf in the DPM matrix and each GENCO participates in LFC as defined by the following ACE participation factor apf_{11} = apf_{12} = 0.5 and apf_{21} = apf_{22} = 0.5. The dynamic responses are shown in Fig. 6. From this Fig 6 the corresponding FAI_1, FAI_2, FAI_3 and FAI_4 is calculated.

Case 7: For this case also bilateral transaction on TATRIPS is considered with a modification that the GENCOs in each area participate not equally in LFC and load demand is more than the GENCO in both the areas. But it is assumed that the load demand change occurs in both areas and the sum of the column entries of the DPM matrix is more than unity.

Case 8: Considering in the case 7 again with a modification that DISCO 1 demands 0.1 p.u MW of excess power i.e., ∆Puc_1 = 0.1 p.u MW and ∆Puc_2 = 0.0 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = ∆P_{uc1} + ∆P_{uc2} = 0.15 + 0.0 = 0.15 p.u MW and total load in area 2 = Load of DISCO 3 + Load of DISCO 4 = ∆P_{uc3} + ∆P_{uc4} = 0.05 + 0.15 = 0.2 p.u MW.

Case 9: In the case which similar to case 7 with a modification that DISCO 3 demands 0.1 p.u MW of excess power i.e., ∆Puc_3 = 0.1 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 + Load of DISCO 3 = ∆P_{uc1} + ∆P_{uc2} + ∆P_{uc3} = 0.15 + 0.05 + 0.05 = 0.25 p.u MW.

Case 10: In the case which similar to case 9 with a modification that DISCO 1 and DISCO 3 demands 0.1 p.u MW of excess power i.e., ∆Puc_1 = 0.1 p.u MW and ∆Puc_3 = 0.1 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 + Load of DISCO 3 = ∆P_{uc1} + ∆P_{uc2} + ∆P_{uc3} = 0.15 + 0.05 + 0.05 = 0.25 p.u MW.

Case 11: In the TATRIPS considering all the DISCOs have contract with the GENCOs but GENCO4 is outage in area-2. In this case, the DISCO 1, DISCO 2, DISCO 3 and DISCO 4, demands 0.15 p.u MW, 0.05 p.u MW, 0.15 p.u MW and 0.05 p.u MW from GENCOs as defined by cpf in the DPM matrix (24). The output GENCO4 = 0 p.u MW.

Case 12: Consider in this case which is same as Case 11 but DISCO 1 demands 0.1 p.u MW of excess power i.e., ∆Puc_1 = 0.1 p.u MW and ∆Puc_2 = 0.0 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = ∆P_{uc1} + ∆P_{uc2} = 0.15 + 0.0 = 0.15 p.u MW and total load in area 2 = Load of DISCO 3 + Load of DISCO 4 = ∆P_{uc3} + ∆P_{uc4} = 0.05 + 0.15 = 0.2 p.u MW.

Case 13: This case is same as Case 11 with a modification that DISCO 3 demands 0.1 p.u MW of excess power i.e., ∆Puc_3 = 0.1 p.u MW and ∆Puc_4 = 0.05 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = ∆P_{uc1} + ∆P_{uc2} = 0.15 + 0.05 = 0.2 p.u MW.

Comprehensive Assessment Indices

Apart from the normal operating condition of the TATRIPS few other case studies like one unit outage in an area, outage of one distributed generation in an area are considered individually. With the various case studies and based on their optimal gains the corresponding CAI is obtained as follows.

Case 11: In the TATRIPS considering all the DISCOs have contract with the GENCOs but GENCO4 is outage in area-2. In this case, the DISCO 1, DISCO 2, DISCO 3 and DISCO 4, demands 0.15 p.u MW, 0.05 p.u MW, 0.15 p.u MW and 0.05 p.u MW from GENCOs as defined by cpf in the DPM matrix (24). The output GENCO4 = 0 p.u MW.

Case 12: Consider in this case which is same as Case 11 but DISCO 1 demands 0.1 p.u MW of excess power i.e., ∆Puc_1 = 0.1 p.u MW and ∆Puc_2 = 0.0 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = ∆P_{uc1} + ∆P_{uc2} = 0.15 + 0.0 = 0.15 p.u MW and total load in area 2 = Load of DISCO 3 + Load of DISCO 4 = ∆P_{uc3} + ∆P_{uc4} = 0.05 + 0.15 = 0.2 p.u MW.

Case 13: This case is same as Case 11 with a modification that DISCO 3 demands 0.1 p.u MW of excess power i.e., ∆Puc_3 = 0.1 p.u MW and ∆Puc_4 = 0.05 p.u MW. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = ∆P_{uc1} + ∆P_{uc2} = 0.15 + 0.05 = 0.2 p.u MW.
excess power i.e., $\Delta P_{uc} = 0.1 \text{ p.u MW}$. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = $\Delta P_{l1} + \Delta P_{l4} = 0.15 + 0.05 = 0.2 \text{ p.u MW}$ and total demand in area 2 = Load of DISCO 3 + Load of DISCO 4 = $\Delta P_{l3} + \Delta P_{l4} + \Delta P_{uc} = 0.15 + 0.05 + 0.1 = 0.3 \text{ p.u MW}$

Case 14: In this case which is similar to Case 11 with a modification that DISCO 1 and DISCO 3 demands 0.1 p.u MW of excess power i.e., $\Delta P_{uc} = 0.1 \text{ p.u MW}$ and $\Delta P_{uc} = 0.1 \text{ p.u MW}$. The total load in area 1 = Load of DISCO 1 + Load of DISCO 2 = $\Delta P_{l1} + \Delta P_{l4} = 0.15 + 0.1 = 0.3 \text{ p.u MW}$.

TABLE I Optimized Controller parameters of the TATRIPS

<table>
<thead>
<tr>
<th>Case</th>
<th>$K_{p1}$</th>
<th>$K_{i1}$</th>
<th>$K_{p2}$</th>
<th>$K_{i2}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case 1</td>
<td>0.341</td>
<td>0.459</td>
<td>0.191</td>
<td>0.081</td>
</tr>
<tr>
<td>Case 2</td>
<td>0.384</td>
<td>0.368</td>
<td>0.212</td>
<td>0.096</td>
</tr>
<tr>
<td>Case 3</td>
<td>0.428</td>
<td>0.396</td>
<td>0.236</td>
<td>0.127</td>
</tr>
<tr>
<td>Case 4</td>
<td>0.396</td>
<td>0.421</td>
<td>0.242</td>
<td>0.134</td>
</tr>
<tr>
<td>Case 5</td>
<td>0.412</td>
<td>0.436</td>
<td>0.253</td>
<td>0.139</td>
</tr>
<tr>
<td>Case 6</td>
<td>0.316</td>
<td>0.513</td>
<td>0.121</td>
<td>0.196</td>
</tr>
<tr>
<td>Case 7</td>
<td>0.336</td>
<td>0.527</td>
<td>0.139</td>
<td>0.184</td>
</tr>
<tr>
<td>Case 8</td>
<td>0.341</td>
<td>0.564</td>
<td>0.218</td>
<td>0.171</td>
</tr>
<tr>
<td>Case 9</td>
<td>0.357</td>
<td>0.568</td>
<td>0.247</td>
<td>0.195</td>
</tr>
<tr>
<td>Case 10</td>
<td>0.364</td>
<td>0.571</td>
<td>0.274</td>
<td>0.187</td>
</tr>
<tr>
<td>Case 11</td>
<td>0.384</td>
<td>0.576</td>
<td>0.277</td>
<td>0.175</td>
</tr>
<tr>
<td>Case 12</td>
<td>0.401</td>
<td>0.584</td>
<td>0.279</td>
<td>0.205</td>
</tr>
<tr>
<td>Case 13</td>
<td>0.419</td>
<td>0.587</td>
<td>0.286</td>
<td>0.237</td>
</tr>
<tr>
<td>Case 14</td>
<td>0.462</td>
<td>0.591</td>
<td>0.296</td>
<td>0.244</td>
</tr>
</tbody>
</table>

TABLE II Optimized Controller parameters of the TATRIPS with SMES unit

<table>
<thead>
<tr>
<th>Case</th>
<th>$K_{p1}$</th>
<th>$K_{i1}$</th>
<th>$K_{p2}$</th>
<th>$K_{i2}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case 1</td>
<td>0.256</td>
<td>0.517</td>
<td>0.125</td>
<td>0.117</td>
</tr>
<tr>
<td>Case 2</td>
<td>0.264</td>
<td>0.516</td>
<td>0.139</td>
<td>0.136</td>
</tr>
<tr>
<td>Case 3</td>
<td>0.267</td>
<td>0.553</td>
<td>0.156</td>
<td>0.163</td>
</tr>
<tr>
<td>Case 4</td>
<td>0.271</td>
<td>0.589</td>
<td>0.158</td>
<td>0.213</td>
</tr>
<tr>
<td>Case 5</td>
<td>0.282</td>
<td>0.612</td>
<td>0.161</td>
<td>0.218</td>
</tr>
<tr>
<td>Case 6</td>
<td>0.203</td>
<td>0.645</td>
<td>0.106</td>
<td>0.265</td>
</tr>
<tr>
<td>Case 7</td>
<td>0.217</td>
<td>0.687</td>
<td>0.139</td>
<td>0.284</td>
</tr>
<tr>
<td>Case 8</td>
<td>0.296</td>
<td>0.694</td>
<td>0.143</td>
<td>0.286</td>
</tr>
<tr>
<td>Case 9</td>
<td>0.342</td>
<td>0.701</td>
<td>0.156</td>
<td>0.301</td>
</tr>
<tr>
<td>Case 10</td>
<td>0.351</td>
<td>0.729</td>
<td>0.188</td>
<td>0.323</td>
</tr>
<tr>
<td>Case 11</td>
<td>0.364</td>
<td>0.736</td>
<td>0.195</td>
<td>0.334</td>
</tr>
<tr>
<td>Case 12</td>
<td>0.396</td>
<td>0.743</td>
<td>0.205</td>
<td>0.343</td>
</tr>
<tr>
<td>Case 13</td>
<td>0.425</td>
<td>0.756</td>
<td>0.211</td>
<td>0.355</td>
</tr>
<tr>
<td>Case 14</td>
<td>0.489</td>
<td>0.769</td>
<td>0.218</td>
<td>0.384</td>
</tr>
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</table>

TABLE III Comparison of the system dynamic performance for TATRIPS

<table>
<thead>
<tr>
<th>TATRIPS (Poolco based transaction)</th>
<th>Setting time ($\tau_i$) in sec</th>
<th>Peak over/under shoot</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\Delta F_1$</td>
<td>$\Delta F_2$</td>
</tr>
<tr>
<td>Without SMES units</td>
<td>18.14</td>
<td>17.52</td>
</tr>
<tr>
<td>With SMES unit</td>
<td>14.25</td>
<td>13.89</td>
</tr>
</tbody>
</table>
### TABLE IV (a) Feasible Assessment Indices (FAI) without and with SMES unit (utilization factor K=1) for TATRIPS

<table>
<thead>
<tr>
<th>TATRIPS</th>
<th>Feasible Assessment Indices (FAI) based on control input deviations ($\Delta P_c$) without SMES unit (utilization factor K=0)</th>
<th>Feasible Assessment Indices (FAI) based on control input deviations ($\Delta P_c$) with SMES unit (utilization factor K=1)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$e_1$</td>
<td>$e_2$</td>
</tr>
<tr>
<td>Case 1</td>
<td>0.975</td>
<td>0.886</td>
</tr>
<tr>
<td>Case 2</td>
<td>1.086</td>
<td>0.967</td>
</tr>
<tr>
<td>Case 3</td>
<td>1.326</td>
<td>1.025</td>
</tr>
<tr>
<td>Case 4</td>
<td>1.185</td>
<td>1.322</td>
</tr>
<tr>
<td>Case 5</td>
<td>1.461</td>
<td>1.375</td>
</tr>
<tr>
<td>Case 6</td>
<td>0.926</td>
<td>0.875</td>
</tr>
<tr>
<td>Case 7</td>
<td>1.126</td>
<td>0.916</td>
</tr>
<tr>
<td>Case 8</td>
<td>1.325</td>
<td>1.025</td>
</tr>
<tr>
<td>Case 9</td>
<td>1.234</td>
<td>1.327</td>
</tr>
<tr>
<td>Case 10</td>
<td>1.376</td>
<td>1.345</td>
</tr>
</tbody>
</table>

### TABLE IV (b) Feasible Assessment Indices (FAI) without and with SMES unit (utilization factor K=0.75) for TATRIPS

<table>
<thead>
<tr>
<th>TATRIPS</th>
<th>Feasible Assessment Indices (FAI) based on control input deviations ($\Delta P_c$) without SMES unit (utilization factor K=0)</th>
<th>Feasible Assessment Indices (FAI) based on control input deviations ($\Delta P_c$) with SMES unit (utilization factor K=0.75)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$e_1$</td>
<td>$e_2$</td>
</tr>
<tr>
<td>Case 1</td>
<td>0.975</td>
<td>0.886</td>
</tr>
<tr>
<td>Case 2</td>
<td>1.086</td>
<td>0.967</td>
</tr>
<tr>
<td>Case 3</td>
<td>1.326</td>
<td>1.025</td>
</tr>
<tr>
<td>Case 4</td>
<td>1.185</td>
<td>1.322</td>
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<tr>
<td>Case 5</td>
<td>1.461</td>
<td>1.375</td>
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<tr>
<td>Case 6</td>
<td>0.926</td>
<td>0.875</td>
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<tr>
<td>Case 7</td>
<td>1.126</td>
<td>0.916</td>
</tr>
<tr>
<td>Case 8</td>
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<td>1.025</td>
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<tr>
<td>Case 9</td>
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<td>1.327</td>
</tr>
<tr>
<td>Case 10</td>
<td>1.376</td>
<td>1.345</td>
</tr>
</tbody>
</table>

### TABLE IV(c) Feasible Assessment Indices (FAI) without and with SMES unit (utilization factor K=0.5) for TATRIPS

<table>
<thead>
<tr>
<th>TATRIPS</th>
<th>Feasible Assessment Indices (FAI) based on control input deviations ($\Delta P_c$) without SMES unit (utilization factor K=0)</th>
<th>Feasible Assessment Indices (FAI) based on control input deviations ($\Delta P_c$) with SMES unit (utilization factor K=0.5)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$e_1$</td>
<td>$e_2$</td>
</tr>
<tr>
<td>Case 1</td>
<td>0.975</td>
<td>0.886</td>
</tr>
<tr>
<td>Case 2</td>
<td>1.086</td>
<td>0.967</td>
</tr>
<tr>
<td>Case 3</td>
<td>1.326</td>
<td>1.025</td>
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<tr>
<td>Case 6</td>
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<td>Case 8</td>
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<tr>
<td>Case 9</td>
<td>1.234</td>
<td>1.327</td>
</tr>
<tr>
<td>Case 10</td>
<td>1.376</td>
<td>1.345</td>
</tr>
</tbody>
</table>
### TABLE V (a) Comprehensive Assessment Indices (CAI) without and with SMES unit (utilization factor K=1) for TATRIPS

<table>
<thead>
<tr>
<th>TATRIPS</th>
<th>Comprehensive Assessment Indices (CAI) based on control input deviations ($\Delta P_c$) without SMES unit (utilization factor K=0)</th>
<th>Comprehensive Assessment Indices (CAI) based on control input deviations ($\Delta P_c$) with SMES unit (utilization factor K=1)</th>
</tr>
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<tbody>
<tr>
<td>$\varepsilon_5$</td>
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<td>$\varepsilon_7$</td>
</tr>
<tr>
<td>Case 11</td>
<td>1.134</td>
<td>1.517</td>
</tr>
<tr>
<td>Case 12</td>
<td>1.524</td>
<td>1.524</td>
</tr>
<tr>
<td>Case 13</td>
<td>1.345</td>
<td>1.623</td>
</tr>
<tr>
<td>Case 14</td>
<td>1.627</td>
<td>1.735</td>
</tr>
</tbody>
</table>

### TABLE V (b) Comprehensive Assessment Indices (CAI) without and with SMES unit (utilization factor K=0.75) for TATRIPS

<table>
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<th>TATRIPS</th>
<th>Comprehensive Assessment Indices (CAI) based on control input deviations ($\Delta P_c$) without SMES unit (utilization factor K=0)</th>
<th>Comprehensive Assessment Indices (CAI) based on control input deviations ($\Delta P_c$) with SMES unit (utilization factor K=0.75)</th>
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<td>$\varepsilon_7$</td>
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<tr>
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<td>1.517</td>
</tr>
<tr>
<td>Case 12</td>
<td>1.524</td>
<td>1.524</td>
</tr>
<tr>
<td>Case 13</td>
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<td>1.623</td>
</tr>
<tr>
<td>Case 14</td>
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</tbody>
</table>

### TABLE V (c) Comprehensive Assessment Indices (CAI) without and with SMES unit (utilization factor K=0.5) for TATRIPS

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<thead>
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<th>TATRIPS</th>
<th>Comprehensive Assessment Indices (CAI) based on control input deviations ($\Delta P_c$) without SMES unit (utilization factor K=0)</th>
<th>Comprehensive Assessment Indices (CAI) based on control input deviations ($\Delta P_c$) with SMES unit (utilization factor K=0.5)</th>
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</thead>
<tbody>
<tr>
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<tr>
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<td>1.517</td>
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<tr>
<td>Case 12</td>
<td>1.524</td>
<td>1.524</td>
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<tr>
<td>Case 13</td>
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<td>1.623</td>
</tr>
<tr>
<td>Case 14</td>
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</tbody>
</table>

### TABLE V (d) Comprehensive Assessment Indices (CAI) without and with SMES unit (utilization factor K=0.25) for TATRIPS

<table>
<thead>
<tr>
<th>TATRIPS</th>
<th>Comprehensive Assessment Indices (CAI) based on control input deviations ($\Delta P_c$) without SMES unit (utilization factor K=0)</th>
<th>Comprehensive Assessment Indices (CAI) based on control input deviations ($\Delta P_c$) with SMES unit (utilization factor K=0.25)</th>
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</thead>
<tbody>
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<tr>
<td>Case 11</td>
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<td>Case 12</td>
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<tr>
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<td>1.623</td>
</tr>
<tr>
<td>Case 14</td>
<td>1.627</td>
<td>1.735</td>
</tr>
</tbody>
</table>
Fig. 5 (a). $\Delta F_1$ (Hz) Vs Time (s)

Fig. 5 (b). $\Delta F_2$ (Hz) Vs Time (s)

Fig. 5 (c). $\Delta \text{P_{tie12}}$ (p.u.MW) Vs Time (s)

Fig. 5 (d). $\Delta \text{P_{c1}}$ (p.u.MW) Vs Time (s)

Fig. 5 (e). $\Delta \text{P_{c2}}$ (p.u.MW) Vs Time (s)

Fig. 5. Dynamic responses of the frequency deviations, tie-line power deviations and Control input deviations for TATRIPS in the restructured scenario-1 (poolco based transactions)
7 Conclusion

This paper proposes the design of various Power System Ancillary Service Requirement Assessment Indices (PSASRAI) which highlights the necessary requirements to be adopted in minimizing the control input deviations thereby reducing the frequency deviations, tie-line power deviation in a two-area Thermal reheat interconnected restructured power system to ensure the reliable operation of the power system. The PI controllers are designed using BFO algorithm and implemented in a TATRIPS without and with SMES unit. This BFO Algorithm was employed to achieve the optimal parameters of gain values of the various combined control strategies. As BFO is easy to implement without additional computational complexity, with this algorithm quite promising results can be obtained and ability to jump out the local optima. Moreover, Power flow control by SMES unit is also found to be efficient and effective for improving the dynamic performance of load frequency control of the interconnected power system than that of the system without SMES unit. From the simulated results it is observed that the restoration indices calculated for
the TATRIPS with SMES unit indicates that more sophisticated control for a better restoration of the power system output responses and to ensure improved Power System Ancillary Service Requirement Assessment Indices (PSASRAI) in order to provide good margin of stability than that of the TATRIPS without SMES unit.

References:


**APPENDIX - A**

**A.1 Data for Thermal Reheat Power System [14]**

Rating of each area = 2000 MW, Base power = 2000 MVA, f = 60 Hz, R1 = R2 = R3 = R4 = 2.4 Hz / p.u.MW, Tg1 = Tg2 = Tg3 = Tg4 = 0.08 s, T r1 = T r2 = T r3 = T r4 = 0.3 s, K p1 = K p2 = 120Hz/p.u.MW, T p1 = T p2 = 20 s, β1 = β2 = 0.425 p.u.MW / Hz, K r1 = K r2 = K r3 = K r4 = 0.5, 2πT r2 = 0.545 p.u.MW / Hz, a r2 = -1.

**A.2 Data for the SMES unit [25]**

Ido = 4.5 kA, L = 2.65 H, Ko = 6000 kV/Hz, Kid = 0.2 kV/kA, K_{SMES} = 100 KV/ unit MW, T_{de} = 0.03s