

# Algorithms for discovering Regular Plans in Wireless Mobile Environment

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*Abstract:* - The emerging wireless communication technology gives mobile financial services, location-based services by providing users with the capability of accessing data at any time and place. The broadcast problem including the plan design is considered. The data are inserted and numbered at a predefined order into customized size relations. The server fetches the requests and broadcasts the data to the air. A set of algorithms can guarantee, the creation of a full Regular Broadcast Plan (RBP), for the server with equal spacing repeated instances of items using single or multiple channels. First, the Basic regular (BRA) and the Partition Value algorithm (PVA), can provide a static and dynamic RBP construction with multiple constraints solutions respectively. PVA can also build the grouping of strong relations with minimum number of channels. Second, the Grouping Dimensioning Algorithm (GD) provides dynamic solutions and, creates groups with predefined average access time, considering economy of channels. The Cuchoo Search Algorithm (CS) is selected for optimization. CS can discover the RBPs with minimum number of channels. Theorems for discovery RBPs with their criteria are used for preparing the conditions for developing the CS algorithms. Servers with these advantages, in addition to their self-monitoring and self-organizing, will have the ability for channel availability and lower energy consumption by using smaller number of channels. Simulation results are provided.

*Key-Words:* -Broadcasting, Mobile Computing, Cuchoo Algorithm, Broadcast Plan, Relations, Grouping, Wireless Network.

## 1 Introduction

Mobile computing is based on the communication between clients and the large scale distributed database. An efficient broadcast schedule program minimizes the client expected delay, which is the average time spent by a client before receiving the requested items. The expected delay of data items is called waiting time. The broadcast channels are also known as “broadcast disks” [1]. There are three basic data broadcasting design methods: the flat, the skewed and the regular. The first two have attracted a great amount of attention [1],[2],[3],[4],[8]. The objective of broadcasting plan is to reduce the expected delay. In this context and based on data popularity, partition methods have been developed [2]. For the flat design the bigger the size of the data set to be transmitted by the server, the higher the expected delay. In large cycles of a flat design users have long wait before getting data that had preciously missed. A higher number of channels is used, for the long broadcast cycle, to reduce the waiting time. For the skewed design, the most frequently requested data are directed to fast

channels, and the cold data to slow channels. The regular design is based on the attribute of equal spacing and offers channel availability and energy conservation. It outperforms the flat one by providing shorter average waiting time for both single and multiple channels. In our work it is considered that the users of the popular sets can find their data in the same channel while the users of the last set (most unpopular) have to use other channels as well. In previous work [5], a method used was based on the known size of data sets. The server works with a set of different message (service) queues and has to define the size of data of each set to be processed in order to create an RBP. This problem becomes complicated when there are many categories of data sets and the need for RBPs solution becomes more necessary. The correct selection of the size of data becomes key for an RBP creation. It is considered that there are queues for the various data sets and the scheduler gets packets of them in a cycle (starting from the frequently requested data to the cold data) and transfers them into the main queue. The main purpose of this work

is to prepare a framework that will include the structure of the data, the server operations in order to provide an RBP. To this end, some theorems have been developed. Data can be sent by a single channel or a set of channels. Finding the number of channels that can send a group of data, providing also the equal spacing of repeated instances of items, could be a very interesting issue. GDA that belongs to the Compound Relations Algorithms (CRA) finds the minimum number of channels that produce an efficient RBP directly. The surplus of the available channels of both grouping algorithms may be used for other RBP.

The Cuckoo Search Algorithm (CS) based on the Levy flight behavior and brood parasitic behavior is introduced [7]. The CS has been proven to deliver excellent performance, among others, in function optimization and neural networks training and engineering design.

For the server there is a need to discover Regular Plans for answering the users' mobile queries. The problem stated on the computation of the size of data of different services so that an RBP or RBPs will be feasible. An RBP is considered feasible if it follows the criteria, as will be developed next and with the smaller number of channels. For this purpose a framework with a set of service queues along with the main queue is considered. In addition, solutions for low and high capacity channels are given based on the grouping length. A Cuckoo Search for Regular Plans (CSR) is developed which can find solutions for servers with a diversity of services and a big size of messages. Solutions with equal and different subrelations are provided.

The paper is organized as follows. In Section 2, and 3 the model description with some analytical results is provided. Sections 4, and 5 the CS algorithm and the CSR are developed, respectively. Finally, simulation results are provided in Section 6.

## 2 Model Description

This section contains the definitions, relations and the criteria for the Broadcast Plan.

The likelihood of having a full BP, is studied by using relations iteratively starting from the last set  $S_3$ . For this purpose three sets  $S_i$  ( $i=1,2,3$ ) with their sizes  $S_{is}$  so that  $S_{1s} \leq S_{2s} \leq S_{3s}$  are considered. A set of relations can be created using the  $S_1, S_2, S_3$ , considering different number of relations ( $n_{rel}$ ) and subrelations in each set ( $i$ -subrelation,  $i=1,2,3$ ). It is assumed that there are three or four subrelations per

relation. For sets  $S_i$  ( $i=1,2$ ) items will be sent at least twice, while for the last one  $S_3$  at least one.

A set of *definitions* have been developed in regards to the construction of and RBP:

(1) the size of relation ( $s_{rel}$ ) is the number of items that belong to the relation, a subrelation is a part of a relation.

(2) full BP (FBP): is the broadcast plan, BP, without any empty slot

(3) regular BP (RBP): the FBP with equal spacing property

(4) item multiplicity ( $it_{mu}$ ): the number of items repeated in a subrelation

(5) different composition RBP: is an RBP that has the same number of channels when there is a swap between  $s_{sum_i}$  and  $ps_i$ . See example 4.

(6) grouping length ( $gl$ ) it is a divisor  $S_{ks}(1, \dots, k)$

(7) partition value ( $pv$ ): is the value with:  $pv_i | S_{is}$  and  $pv_i | gl$ .

(8) number of channels ( $nc$ ):  $S_k / gl$  (where  $S_k$  is the last set)

A set of *criteria* have also been developed:

(1) The criterion of homogenous grouping ( $chg$ ): when  $pv_i | gl$ .

(2) The criterion of multiplicity constraint ( $cmc$ ) or differential multiplicity: This happens if:  $it_{mu_{i+1}} < it_{mu_i}$  ( $i=1, \dots, n-1$ ).

(3) The criterion of PV ( $cpv$  or  $pvi$ ): when:  $pv_i < pv_j$  (for  $i < j$ ).

The  $chg$  along with  $cpv$  can guarantee the  $cmc$  for different multiplicity (Theorem 1) and because of that the  $cmc$  is not necessary to be examined.

More details are in (5).

*Example 1:* If  $S_{3s} = 80$ ,  $gl = 40$ , considering that  $s_{sum_3} = 8$  then  $pv_3 = 10$  ( $= 80/8$ ). Hence  $pv_3 | S_{3s}$  and  $pv_3 | gl$ .

These definitions and criteria are used in the Tabu process for discovering RBPs.

A set of *grouping* operations for GDA:

Having ready the RBP then it is possible to combine the relations and create groups of relations depending on the needs of the system (number of channels, and the bounds for  $AWTi$ ,  $i=3$ ). For the grouping relations the following definitions are needed:

(1) *Homogenous grouping (hog)*: it consists of a set of strong relations and the  $i$ -subrelations contain all their items of  $S_i$  ( $i=1,2$ ) without common items. In other words:  $\cup(i\_subrelation) = S_i$  and  $\cap(i\_subrelation) = \{\emptyset\}$ ,  $i=1,2,3$ . The same number of relations and all of them participate in the grouping process and symmetry load to the channels is provided. It provides the perfect mapping.

(2) *Semi-homogenous grouping (shog)*: is the case where the grouping is the same like the homogenous

but finally we have asymmetry load to the channels. More relations are mapping to some channels and less relations to some others.

(3) *Heterogeneous grouping (heg)*: it consists of a set of weak relations where:  $\cup(i\_subrelation) \neq S_i$  and  $\cap(i\_subrelation) \neq \{\emptyset\}$ ,  $i=1,2,3$ . All the relations may participate in the grouping process.

(4) *Integrated relations (int\_rel)* is a set of relations so that the union of items in the  $i\_sub$  relations ( $i=1,2$ ) to give the  $S_1$  and  $S_2$ . In other words the  $\cup(i\_subrelation) = S_i$  ( $i=1,2$ ).

(5) *Grouping Factor (gf)*: is the ratio of the number of integrated relations divided by the number of channels. It is used only when  $gt$  is integer and there are more channels than the set of integrated relations. In that case we perform an homogenous grouping. If  $gf=1$  then we have perfect matching (one channel for each  $ir$ ) and this does not provide service discrimination, since all the items of the relation have the same multiplicity.

(6) *Homogenous grouping by gf (hgf)*: Is when the  $gf > 1$ ,  $gf \in I$ . For example: when there are 10  $ir$  and 5 channels, then the  $hgf$  give us the best matching, 2  $ir$  for each channel.

### 3 BRA

The BRA is based on the conditions to find an RBP and basically works with three sets. It tries to find item multiplicity for the sets, and makes groups of relations using single or multiple channels. It starts with the discovery of an RBP with the smallest number of channels. Grouping methods for the composition of integrated relations with the case of the perfect or approximate matching are also examined. More details are in [5].

### 4 PVA

The PVA gives answers for cases of minimum number channels. It works with no grouping or RGA. For all the predefined number of integrated relations ( $d_4$ ) we try to discover the values of  $pv_i$  ( $i \leq n$ ) so that the criterion of homogenous grouping is valid and the multiplicity constraint is satisfied.

*PVA : input*:  $S_1, S_2, S_3, S_4$ ,  $S_i$  ( $i \leq 4$ ),  $n\_ch$ : the # of channels,  $exist\_v$ : the variable for  $chg$

*output*: the homogenous grouping for multiple channels

find the divisors set  $D_4$  of  $S_4$  ( $d_4 \in D_4$ )

find the divisors of the  $S_1, S_2, S_3$  (in decreasing order)

// $D_3$  for  $S_3$ ,  $D_2$  for  $S_2$ ,  $D_1$  for  $S_1$

// $d_3 \in D_3$ ,  $d_2 \in D_2$ ,  $d_1 \in D_1$

find the  $n\_ch = D_4 / d_4$

for each divisor ( $d_4$ ) of set  $S_4$  (a)

for all  $S_i$  ( $i \leq 4$ )

(b)

{ //define the  $s\_sum_i = d_i$  ( $i < 4$ )

$s\_sum_i = d_i$  ( $i < 4$ )

$pv_i = S_{is} / s\_sum_i$

$it\_mu_i = d_4 / pv_i$

//examine the  $chg$

$exist\_v = "y"$

while ( $it\_mu_i \notin I$ ) // ( $i < 4$ )

{  $j=i$ ;  $exist\_v = "n"$ ;

//find new  $s\_sum_j$ ,

go to (b) }

if  $exist\_v = "y"$

//examine the multiplicity constraint

$it\_mu\_all = "y"$

if ( $it\_mu_{i+1} < it\_mu_i$ )

{ the PVA provides solution for  $S_i, S_{i+1}$

homogenous grouping and for  $n\_ch$  }

else { //find another  $d_4$

$it\_mu\_all = "n"$ ;

go to (a) }

if  $it\_mu\_all = "y"$

{ the PVA provides  $hg$  for all the sets with

$n\_ch$  }

*Example 2*: Consider the sets:  $S_1s=10, S_2s=20, S_3s=40, S_4s=120$ . The divisor of  $S_4s$  are:  $D_4=\{20,30,40\}$ . For  $d_4=20$  the number of channels,  $n\_ch=120/20=6$ .

The divisors of  $S_i$  ( $i \leq n$ ),  $D_3=\{8,5\}$ ,  $D_2=(5,4), D_1=\{5,2\}$ .

Taking:  $d_3=8, d_2=5, d_1=5$ . Considering as  $n_4=d_4=20$ ,  $s\_sum_3=8(=d_3)$ ,  $S\_sum_2=5(=d_2)$ ,  $s\_sum_1=5(=d_1)$  then we have:

$pv_3=40/8=5$ , and  $it\_mu_3=20/5=4$

$pv_2=20/5=4$ , and  $it\_mu_2=20/4=5$

$pv_1=10/5=2$ , and  $it\_mu_1=20/2=10$

So the  $chg$  and the  $cmc$  are valid ( $it\_mu_3 < it\_mu_2 < it\_mu_1$ )

If the divisors of  $S_4$  are at a decreasing order (e.i., 60, 40, 20) the  $n\_cl$  will take the lower value. This is used when the design of RBP is only for a minimum number of channels.

The RBP for all the available channels can be achieved when the divisor of  $S_4$  are at an increasing order. This comes from the  $n\_cl$  formula ( $D_4 / d_4$ ).

### 5 GDA

The GDA works with creation of the groups using fewer channels. Economy of channels is very important factor for a large size of broadcast cycle. The grouping is made so that the AWT3 becomes

less than a predefined average waiting time for  $S_3$  data.

GDA:input:n\_rel: # of relations from PVA

n\_rel\_per\_s: is the integrated # relations for  $S_2$

n\_ch: #of channels that provide RBP,

pre\_av\_wt<sub>3</sub>: is the predefined aver. waiting time for the  $S_3$

n\_int\_rel: is # of integrated relations from a RBP

variables: AWT<sub>3</sub>: the aver. waiting time for the concatenated relations for data of  $S_3$

output: min\_n\_used\_ch : the min # of channels that will be used with predefined AWT<sub>3</sub>

for (i= 2: n\_ch; i++)

```
{
n_int_rel = n_rel / n_rel_per_s
```

```
if (n_int_rel = 2p, p ∈ I ) (A)
```

```
{ findki the integer divisors of n_int_rel
```

```
// k1>k2>k3>...>kn, K={k1,k2,k3,...,kn }
```

```
for each k ∈ K // # of channels
```

```
{ ma= n_int_rel / k
```

```
grouping by m integrated relations and create the
k concatenated relations
```

```
if (AWT3 ≤ pre_av_wt3)
```

```
{ min_n_used_ch = k ;
```

```
send k concatenated relations to k channels}
```

```
} } }
```

```
if (n_int_rel = 2p+1, p ∈ I )
```

```
{ we work with 2p integrated relations as in (A)
```

```
and the last one (the 2p+1) is added to the last
```

```
channel }
```

```
} // end for
```

*Example 3:* Let us consider  $S_1 = 1$ ,  $S_2 = \{2,3,4\}$ ,  $S_3 = \{5, \dots, 76\}$  with:  $S_{1s} = 1$ ,  $S_{2s} = 3$ ,  $S_{3s} = 72$ ,  $pre\_av\_wt_3 = 40$ . Here  $S_{3s} \gg S_{2s} \gg S_{1s}$ . Using PVA we have  $k = 24$  ( $72/3$ ),  $it\_mu_2 = 8(24/3)$ . Hence we have a RBP with  $it\_mu_2 = 8$ , and 24 lines. The 24 relations(n\_rel) are (1,2,5,6,7), (1,3,8,9,10), (1,4,11,12,13), (1,2,14,15,16), ..., (1,4,74,75,76). The 8 integrated relations (with  $n\_rel\_per\_s = 3$ ) can be created from the 24 relations are: ((1,2,5,6,7), (1,3,8,9,10), (1,4,11,12,13)), ..., ((1,2,68,69,70), (1,3,71,72,73), (1,4,74,75,76)). If a single channel is used,  $AWT_3 = 72$  and  $72 > 40$  and grouping is needed with multiple channels in order to have less  $AWT_3$ .

We have  $n\_int\_rel = 8$  ( $24/3$ ). The int. divisors of 8: 4,2.

For  $k=4$ ,  $ma = 2$  ( $8/4$ ) we have the grouping integrated relations for 2 channels as follows:

*channel 1:* ((1,2,5,6,7), (1,3,8,9,10), (1,4,11,12,13), (1,2,14,15,16), (1,3,17,18,19), (1,4,20,21,22), (1,2,23,24,25), (1,3,26,27,28), (1,4,21,30,31), (1,2,32,33,34), (1,3,35,36,37), (1,4,38,39,40)).

*channel 2:* ((1,2,41,42,43), (1,3,44,45,46), (1,4,47,48,49), (1,2,50,51,52), (1,3,53,54,55), (1,4,56,57,58), (1,2,59,60,61), (1,3,62,63,64), (1,4,65,66,67), (1,2,68,69,70), (1,3,71,72,73), (1,4,74,75,76)).

The  $AWT_3$  is: 58. Since  $58 > 40$  a new loop for  $k=4$  is needed.

For  $k=4$ ,  $m=4$  ( $8/2$ ) we have the four integr. relations

for four channels: *channel 1* : ((1,2,5,6,7), ..., (1,4,20,21,22)),

*channel 2:* ((1,2,23,24,25), ..., (1,4,38,39,40)),

*channel 3:* ((1,2,41,42,43), ..., (1,4,56,57,58),

*channel 4:* ((1,2,59,60,61), ..., (1,4,74,75,76)).

The  $AWT_3 = 28 < 40$ . Hence, the minimum number of channels is: 4 and this can guarantee the existence of RBP (keep the service discrimination for all the sets).

## 6 Analytical Results

The previous analysis for RBP was based on a certain size of various sets given also the gl. A basic theorem dealing with the criteria (cmc, and pvi) was developed. These theorems are fundamentals for the characteristics of an RBP. To this end, they are referred in this work.

*Theorem1* : Let us consider the case of multiple channel allocation with different multiplicity of sets (such as:  $S_1, S_2, S_3$ ). Then, if  $pvi | d_4$ , the validity of multiplicity constraint ( $it\_mu_{i+1} < it\_mu_i$  ( $i=1, \dots, k-1$ )) can be achieved from the pv criterion ( $pv_i < pv_{i+1}$ ,  $i < k$ ,  $k = \#sets$ ). Similarly the pv criterion can guarantee the multiplicity constraint criterion.

*Proof:* Lets prove that if  $pv_i < pv_{i+1}$  (1) then  $it\_mu_i > it\_mu_{i+1}$ . (2). From (1)  $\Rightarrow 1/pv_i > 1/pv_{i+1} \Rightarrow d_4/pv_i > d_4/pv_{i+1}$ . If  $(d_4/pv_i) \in I$ ,  $\Rightarrow it\_mu_i > it\_mu_{i+1}$ . Following the reverse order we can get from (2) to (1). So it is not necessary to examine the multiplicity criterion and the pv criterion can provide the multiplicity.

*Example 4:* Four sets are considered:  $S_1, S_2, S_3, S_4$  with  $S_{1s} = 10$ ,  $S_{2s} = 20$ ,  $S_{3s} = 40$ ,  $S_{4s} = 120$ . If  $gl = 20$  ( $20$  is a divisor of  $120$ ) then  $S_{1s} / gl$ ,  $S_{2s} / gl$ ,  $gl / S_{3s}$ . The chg exists. The number of channels is:  $nc = 120/20 = 6$ . Considering  $s\_sum1 = 5$ ,  $s\_sum2 = 5$ ,  $s\_sum3 = 8$  then  $pv1 = 10/5 = 2$ ,  $pv2 = 20/5 = 4$ ,  $pv3 = 40/8 = 5$ . We have  $pv1 < pv2 < pv3$  (pv criterion) and since  $pv1 | 20$ ,  $pv2 | 20$ ,  $pv3 | 20$  (or  $d_4 | pv_i$ )  $\in I$ ) then the chg is valid and an RBP can be constructed. From this process it is evident that it is not necessary to test the cmc.

After this short introduction and for framework construction purposes new analytical results are needed.

*Theorem 2:* The grouping length (gl or d4) comes from :  $d4=k \cdot \max(\text{PAVi})$ . Where  $k \in I$  and plays a role to the capacity and the number of channels.

If  $k=1$  then the S4 (the last or cold set) does not repeated in the broadcasting cycle. (low capacity channel) and larger number of channels are needed to send all the S4 data. Increasing the k then less number of channel with more capacity is needed.

*Example 3:* From Example 2, the  $\max(\text{pvi}) = 5$ . If  $k=1$ , considering that a unit is served for each relation (or  $s_{\text{sum}}$ ), it will need  $n_{\text{ch}} = 120/5 = 24$  channels (low capacity channel). But if  $gl=20$  (20 is a divisor of 120) then  $n_{\text{ch}} = 120/20 = 6$  (fast channels)

*Theorem 3:* The size of data for a RBP, can be multiple of the size data of S1. It is considered that S4 has unit service.

*Proof:* the data with sizes:  $S1s, S2s = k S1s, S3s = m S1s$  provide the needed structure for RBP directly. Assuming  $s_{\text{sum}1} = S1s, s_{\text{sum}2} = S1s$  and  $S3s = S1s$ , the  $\text{PAV}1 = 1, \text{PAV}2 = k, \text{PAV}3 = m$ . If  $k/d4$  and  $m/d4$  and  $k < m$ , the criteria will be valid and an RBP exists.

Theorem 3 is the necessary condition in order to have RBP.

*Theorem 4: (for equal size of subrelations)* The size of data can have some equal factors after their factorization. This property can provide an RBP if the non common factors are multiple. (for the same size of subrelations).

*Proof:* let's consider the size of the data:  $S1s(= \text{non}1 \cdot \text{com}1), S2s(\text{non}2 \cdot \text{com}2), S3s(\text{non}3 \cdot \text{com}3), S4s$ . If  $\text{com}1 = \text{com}2 = \text{com}3$  then the  $s_{\text{sum}1} = s_{\text{sum}2} = s_{\text{sum}3} = \text{com}1$ . Moreover if  $\text{non}2 | \text{non}1, \text{non}3 | \text{non}2$  then an RBP is visible since the two criteria are valid.

*Example 5:* Let's  $S1s=10, S2s=30, S3s=60, S4s=120$ . The factorization gives:  $S1s=2 \cdot 5, S2s=3 \cdot 2 \cdot 5, S3s=3 \cdot 2 \cdot 2 \cdot 5$ . The common factor is  $2 \cdot 5 (=s_{\text{sum}i})$  and the non common factors are: 1, 3, 6. These are divisible numbers. Hence an RBP exists with  $\text{PAV}1=1, \text{PAV}2=3, \text{PAV}3=6$ . For the d4 if  $k=1$  then  $d4=6$  (low capacity channel).

*Theorem 5: (for non equalsubrelations)* After the factorization an RBP is feasible when the PAV criterion is valid and a choice for gf (or d4) can be made.

*Example 6:* When subrelations of different size are used. Let's :  $S1s=5, S2s=6, S3s=6$ , and  $\text{PAV}1=2, \text{PAV}2=5, \text{PAV}3=10$ . For d4 if  $k=1$  then  $d4=10$ . (low capacity). In addition, the size of the data sets is not

necessary to be multiple of each other and they can use different subrelations.

*Example 7:* Let's  $S1s=20, S2s=35, S3s=48, S4s=120$ . The factorization gives:  $S1s=4 \cdot 5, S2s=5 \cdot 7, S3s=6 \cdot 8$  and  $\text{PAV}1=4, \text{PAV}2=5, \text{PAV}3=6$ . The subrelations are:  $s_{\text{sub}1}=5, s_{\text{sub}2}=7, s_{\text{sub}3}=8$ . If  $k=1$  then  $d4=6$  and  $n_{\text{ch}} = 120/6 = 20$ . (low capacity channels). If  $k=20$  then  $n_{\text{ch}} = 120/20 = 6$  (fast channels).

Theorem 5 provides a new criterion for searching with CS. This means that for the case of different subrelations after the factorization it needs: (a) the non common factors has to follow the pavi criterion ( $\text{pavi} < \text{pavj}$ , for  $i < j$ ), (b) the value of gf can be discovered so that  $gf | S4s$ , and  $\text{pavi} | gf$  or  $\max(\text{pavi}) = gf$  (c) the value of k depends on the available channels. This new criterion is called as *compound criterion* and it is used from CS.

## 7 CS

The CS can be directly applied to virtually any kind of optimization problem. We can state most of these problems in the following form, where "optimize" means to minimize or maximize:: Here is how to optimize (minimize the number of channels) for the construction of the RBPs:

$$\text{optimize } f(x) = (f_1(x), f_2(x), \dots, f_n(x))$$

subject to  $x \in X$

where X represents the feasible space, that is the set of all valid solutions, the solutions that fulfill every constraint of the problem.

The CS is a higher-level metaheuristic procedure for solving optimization problems, designed to guide the search operator in avoiding the traps of local optimality. Cuckoo birds attract attention because of their unique aggressive reproduction strategy. Cuckoos engage brood parasitism. It is a type of parasitism in which a bird (brood parasite) lays and abandons its eggs in the nest of another species [6]. Cuckoo Search algorithm is population based stochastic global search metaheuristics. It is based on the general random walk system which will be briefly described in this chapter. In Cuckoo Search algorithm, potential solutions corresponds to Cuckoo eggs. One approach is to simplify novel Cuckoo Search algorithm through three below presented approximation rules: (1) Cuckoos chose random location (nest) for laying their eggs. Artificial cuckoo can lay only one egg at the time. (2) Elitist selection process is applied, so only the eggs with highest quality are passed to the next

generation (3) Host nests number is not adjustable. Host bird discovers cuckoo egg with probability  $pd \in [0,1]$ . If cuckoo egg is disclosed by the host, it may be thrown away, or the host may abandon its own nest and commit it to the cuckoo intruder.

A simple representation where one egg in a nest represents a solution and a cuckoo egg represents a new solution is used here. The aim is to use the new and potentially better solutions (cuckoos) to replace worse solutions that are in the nests. The random walk is called Lévy flight and it describes foraging patterns in natural systems,

Only two parameters are needed by the algorithm, the discovery rate  $pd \in [0,1]$  and the size of population  $n$ . When  $n$  is fixed,  $pd$  controls the elitism and the balance of randomization and local search. Most notably, an increase in the local search is needed and this is referred in the CSR

### 8 CS for regular plan, PVA, GDA

The theorems apply to CSR for discovering RBPs. It starts with randomly generated initial population. Each individual is evaluated by the fitness function. The fitness function finds the divisors of the  $S_{is}$  (except for the last set size) and test the applicability of the  $pvi$  and  $cmc$  criterion. Individuals are eliminated when they do not follow the fitness function. The next generations are created with the application of the GA operators. The step size for the Levy flight is set to the  $upperbound_i / 100$ . Where of  $upperbound_i$  is the size of each of the set queues. The size of population  $n$ , is the sum of number of available messages in the service queues. CSR : input : initial population of  $n$  host nests (the size of data in the service queues).

output : discover an RBP

Generate initial population of  $n$  host nests  $x_i$

while  $\{ (t < MaxGenerations) \text{ and } (!$

termin.condit.)

    get a cuckoo randomly via Lévy flights

        //in order to find the next sizes of the sets

    evaluate its fitness  $F_i$  //if the numbers follows

        the compound criterion

    randomly choose nest among  $n$  available nests (for example  $j$ )

if  $(F_i > F_j)$  {replace  $j$  by the new solution;}

    fraction  $pd$  of worse nests are abandoned and new nests are being built;

    //search around  $pd$  ( $n * pd$ ) for best nests (A)

    // and replace if a better solution exists(A)

    for the rest of  $n$  keep the best solutions or nests with quality solutions;

rank the solutions and find the current best }//end while

//Post process and visualize results

In the CSR pseudocode, two lines (A) are added to provide local search for best nests in the area around the  $pd$ .

For the PVA the CSPVA is created in analogous way as the CSR. It takes the RBP from the CSR and then it works according to PVA. The multiplicity constraint is the condition that is examined when discovering the  $pvi$  values. Finally, for the GDA the CSGDA has a constraint for the AWT3 and the minimum number of channels.

### 9 Simulation

Our simulation is concentrated on the effectiveness of CSR, CSPVA, CSGDA and BRA for the discovery of RBPs. The items are separated into at most five categories according to their popularity using Zipf distribution. The scenarios are the following:

*Scenario 1: CSR for various sets.* Let's consider 3 groups of sets with their corresponding queue sizes ( $SQ_i$ ). Group 1:  $SQ_3=150, SQ_2=85, SQ_1=40$ , Group 2:  $SQ_4=350, SQ_3=80, SQ_2=62, SQ_1=25$ , and Group 3:  $SQ_5=330, SQ_4=280, SQ_3=260, SQ_2=140, SQ_1=70$ . Group 4:  $SQ_5=350, SQ_4=300, SQ_3=250, SQ_2=130, SQ_1=80$ . The CSR finds the RBPs in shorter time for the Group 1 then Group 2 and finally for Group 3. This happens because there is an increasing amount of services for the various groups. Group 3 and Group 4 have approximately the same values (Fig. 1).

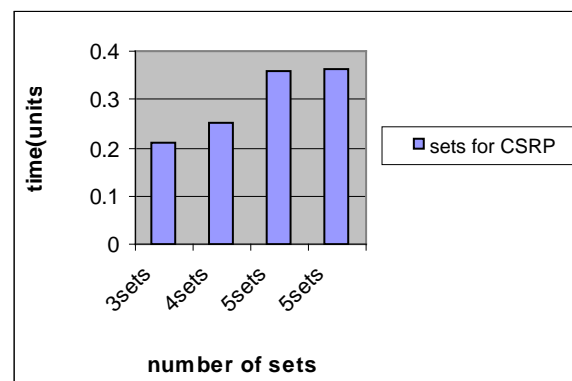


Fig. 1 CSR for various RBPs

*Scenario 2: CSR vs BRA.* Let us consider a group of services with 5 sets and the CSR running against BRA. The CSR outperforms BRA. BRA

has random non local search. CSRP discovers the RBP earlier since it works also with the Levy flights in the next generations and the additional ability for local search (Fig. 2).

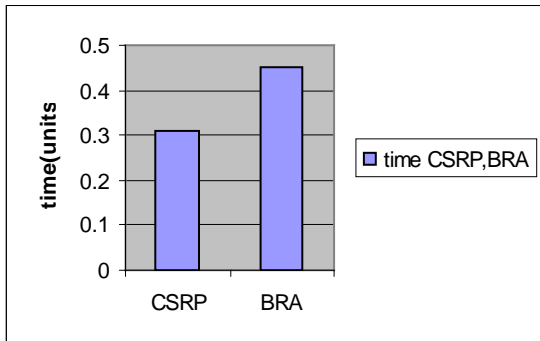


Fig. 2 CSRP vs BRA

*Scenario 3:* Considering  $S_{4s} = 1200$ ,  $S_{3s}=600, S_{2s}=400, S_{1s}= 100$ . The AWT for the S1,S2,S3 remain the same (Fig. 3) because PAV could find the same values of  $pv_i$  for all the number of channels(6,3,2). The  $AWT_4$  has increasing trend, and depends on the number of channels the PAV discovers. The lower the number of channels is the greater the  $AWT_4$ . It is considered that for each relation there is one element (no repetitions).

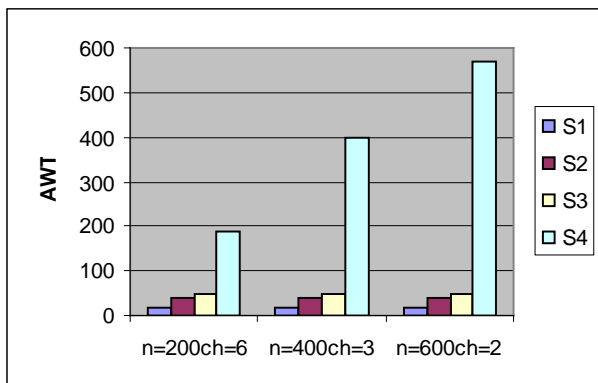


Fig. 3 The AWT for the PAV

*Scenario 4:* Considering the same as the previous scenario with CSPAV running against PAV. SCPAV discover the RBP earlier due to the additional ability for search (Fig. 4)

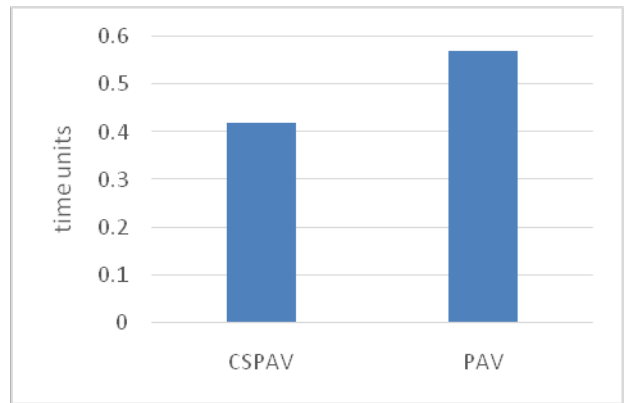


Fig. 4 CSPAV vs PAV

*Scenario 5:* Three set of data are used and three cases (each one for each set) are developed starting from left to right in Fig. 5. All of them have the same  $S_1$  data. The second set has more data (relations) of  $S_3$  and the same size of  $S_2$  data (relations). Because of this, in the second case four channels are used instead of three in order to provide the same  $AWT_3$ . The number of channels are selected according to GDA considering  $pre\_av\_wt_3 = 40sec$ . The third set has more data on  $S_3$  and less data on  $S_2$  comparing with the data of the second set. Because of this there is an increase of  $AWT_3$  (18 sec comparing with 16sec) and a decrease of  $AWT_2$  (from 8sec to 6sec).

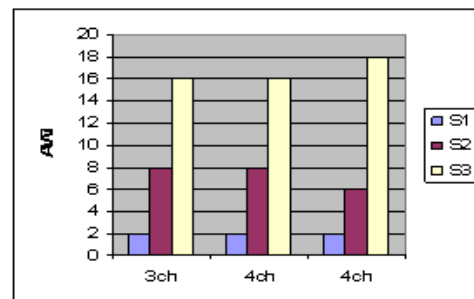


Fig. 5 AWT with GDA grouping

*Scenario 6:* Considering the same as in the previous scenario; the CSGDA supersedes GDA because of the nature of the CSGDA (Fig. 6)

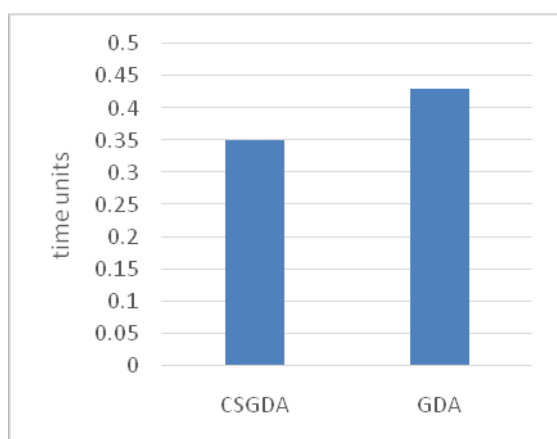


Fig. 6 CSGDA vs GDA

## 10 Conclusion

A set of algorithms that can discover RBP for mobile users using the CS algorithm has been developed. Theorems can discover the sizes of the data sets considering equal and non equal subrelations. The CSRP can discover the sizes of the datasets using the compound criterion and provide an integrated solution to the regular broadcast schedule program minimizing also the client expected delay. It is very effective and flexible for solving hard constraint satisfaction problems and more generally constrained combinatorial search problems. It can provide a new dimension in the design of RBP. The next generation servers, by applying the CSRP, CSPVA, CSGDA will enhance their ability to self-sufficiency, self-monitoring, and they may address quality of service with minimal human intervention. Future work could include the use of other optimization methods for the RP problem

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