Metaheuristic Techniques for the Analog Circuits Performances Optimization -A comparison issue-

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Abstract: - Particle Swarm Optimization (PSO), Ant Colony Optimization (ACO), Genetic Algorithm (GA) and Simulated Annealing (SA) are mostly used as metaheuristic for electronic circuit's performances optimization. Despite their different research techniques, these methods achieve the optimal solution for analog circuit design. The aim of this paper is to make a comparison between the performances reached by those four techniques in the optimal sizing of a CMOS second generation current conveyor (CCII) and an operational amplifier (Op-Amp). The highlighted results obtained by the used algorithms, will be compared in terms of optimum quality, convergence rate and the computing time.

Key-Words: - Swarm Intelligence, Evolutionary Algorithm, Simulated Annealing, Second Generation Current Conveyor, Operational Amplifier.

1 Introduction

Analogue circuit design deals with very complex nonlinear equations, obtaining optimal solution of these equations due to particular constraints in short time and acceptable error is an increasing challenge. It is then generally carried out thanks to the experiment and the intuition of the designer. Automatics procedures for the sizing of analog circuits are mostly suitable in order to design and simulate quickly a given electronic circuit performances and then reducing its time to market [1].

The best-known approaches in literature are based on fixed topologies and/or statistical techniques [2]. They are generally initialized with a "good" solution ("good" DC quiescent point) provided by the skilled analogue designer. The problem with these methods is that they are often very slow and they don't guarantee the convergence to a global optimum. The use of new methods is required. New heuristics based methods able to resolve optimization problems were then introduced [3], among which some are adaptable to many different problems referred to as metaheuristics. Their ability to optimize a problem from a minimum of information is compensated by the fact that they offer no guarantees about the optimality of the best found solution. Only an approximation of the global optimum is given at very reasonable times [4]. Starting from a current given point, in the research space, these methods generate new points by applying operators and by statistically moving toward more optimal places in the research space. Some (meta-)heuristics were proposed in the literature and used by analog designers, such as Tabu Search (TS) [5,6], Genetic Algorithms (GA) [7], Local search (LS) [8], Simulated Annealing (SA) [9], Ant Colony Optimization (ACO) [10-12], Wasp Nest (WN) [13], Bacterial Foraging Optimization (BFO) [14] and Particle Swarm Optimization (PSO) [15,16].

In this work, four different metaheuristic algorithms to solve typical analog circuit sizing problems will be used: Particle Swarm Optimization and Ant Colony Optimization which are derived from the Swarm Intelligence, Genetic Algorithm inspired by mechanisms from evolutionary algorithm and Simulated Annealing based on the physical phenomena. The aim is to compare these four techniques in terms of results quality and computing time for the resolution of analog sizing optimization problems. Two application examples are considered, a second generation current conveyor (CCII) and a two-stage CMOS operational amplifier (Op-Amp).

The rest of the paper is organized as follows. The Section 2 begins by a brief overview of the PSO, ACO, GA and SA techniques. The viability of the proposed algorithms, via some test problems, and the optimization results, obtained by each technique, are presented and compared with each other in section 3 where is also presents the SPICE simulation results which show the validity of the obtained results. In section 4, we give a computing time and a checking of the convergence for the used algorithms. Finally, the major conclusions resulting from this work are presented and discussed.

2 An overview on the used metaheuristics

2.1 Swarm intelligence: PSO and ACO

The most used Swarm Intelligence (SI) techniques in the literature are Particle Swarm Optimization (PSO) and Ant Colony Optimization (ACO) [17-19]. They are artificial intelligence techniques inspired by the collective behaviour of a group of animals such insects, birds and fish.

2.1.1 Particle Swarm Optimization:

The PSO is a stochastic global optimization method based on the social behaviour (bird flocking or fish schooling) and intelligence of swarm searching for the global optimal. This new method was developed by Edward and Kennedy in 1995 [17]. The PSO shares many similarities with evolutionary computation techniques such as Genetic Algorithms (GA). The system is initialized with a population of random solutions and searches for optima by updating solution generations. However, unlike the GA, the PSO has no evolution operators such as crossover and mutation [20].

In the standard PSO, each particle I, is marked by two coordinates, a position-vector $x_{(i)}$ and a velocity a velocity-vector $v_{(i)}$. Each particle remembers its own best position and the global best position (best solution of the entire group).

The equations of velocity and position are illustrated by the following equations:

$$v_{(i+1)} = c \left\{ \omega \ v_{(i)} + c_1 r_1 \left(x_{lbest(i)} - x_{(i)} \right) + c_2 r_2 \left(x_{gbest(i)} - x_{(i)} \right) \right\} \ (1)$$

$$x_{(i+1)} = x_{(i)} + v_{(i)} \tag{2}$$

Where $v_{(i)}$ is the particle velocity and $x_{(i)}$, $x_{lbest(i)}$ and $x_{gbest(i)}$ are respectively the current particle, local best solution and global best solution at the *i*th generation, r_1 and r_2 are uniformly distributed in [0,1], c_1 and c_2 are the learning factors appointing two positive constants defined with an empirical way and according to the relation $c_1 + c_2 \le 4$, ω is the inertia weight; it controls the impact of the previous velocity on the current one, and c is a positive constant named constriction factor and used to control and constrict velocities.

During the iteration time t, the update of the velocity from the previous value to the new one is determined by eq. (1). The new position is then determined by the sum of the previous position and the new velocity by (2). Each particle, which flies over the solution space, remembers the encountered best solution. If this new solution has a cost less than the cost of the current global solution, then this best local solution replaces the best global solution. This process is then iterated many times.

The advantage of the PSO is its easiest implementation and its reduced number of parameters to adjust. The pseudo code of the PSO procedure can be presented as follows:

Initialize the size of the particle swarm and other parameters. Initialize the positions and the velocities for all the particles randomly. Do For each particle Calculate fitness value If the fitness value is better than the best fitness value (pbest) in history set current value as the new pbest End Choose the particle with the best fitness value of all the particles as the gbest For each particle Calculate particle velocity according to (1) Update particle position according to (2) End While maximum iterations or minimum error criteria is not attained

Algorithm 1. Pseudo code of the PSO algorithm

2.1.2 Ant Colony Optimization:

Ant Colony Optimization technique is a metaheuristic stochastic combinatorial computational discipline inspired by the behavior of ant colonies [21,22]. While walking, ants deposit pheromone on the ground marking a path that may be followed by other members of the colony. Shorter paths, as they accumulate pheromone faster than the longer ones, have a higher probability of being used by other ants, which again reinforce the pheromone on that path.

The ACO was first adapted to solve graph related problems, [23,24]. In such problems, ants randomly select the vertex to be visited. When an ant k is in

vertex *i*, the probability of going to vertex *j* is given [23,25] by:

$$p_{ij}^{k} = \begin{cases} \frac{(\tau_{ij})^{\alpha} . (\eta_{ij})^{\beta}}{\sum_{l \in J_{i}^{k}} (\tau_{il})^{\alpha} . (\eta_{il})^{\beta}} & \text{if } j \in J_{i}^{k} \\ 0 & \text{if } j \notin J_{i}^{k} \end{cases}$$
(3)

where J_i^k is the set of neighbors of vertex *i* of the k^{th} ant, τ_{ij} is the amount of pheromone trail on edge (i,j), α and β are weightings that control the pheromone trail and the visibility value, i.e. η_{ij} , given by:

$$\eta_{ij} = \frac{1}{d_{ij}} \tag{4}$$

 d_{ii} being the distance between vertices *i* and *j*. The pheromone values are updated at each iteration by all the m ants that have built a solution in the iteration itself. The pheromone τ_{ii} , which is associated with the edge joining vertices i and j, is updated as follows:

$$\tau_{ij} = (1 - \rho) \tau_{ij} + \sum_{k=1}^{m} \Delta \tau_{ij}^{k}$$
(5)

where ρ is the pheromone evaporation rate, *m* is the number of ants, and $\Delta \tau_{ii}^{k}(t)$ is the quantity of pheromone laid on edge (i, j) by the ant k:

Each ant k will randomly choose a path according to the probability given by expression (3), and form a directed graph while randomly generating a rate of pheromone at the formed graph edges. At each iteration, the path giving the minimum value of the Objective Function (OF) sees its pheromone rate increasing, in contrast with the other paths for which the pheromone rates are partially evaporated with respect to expression (5). The pseudo code of the ACO procedure can be presented as follows:

```
Random initialization of the pheromone value
Do
  For each iteration
    For each ant
       For each variable
        Compute of the probability P according to (3)
        Determine the Pmax
        Deduce the value of Vi
       End
     Compute OF
     End
   Deduce the best OF
   Update pheromone values according to (5)
  End
  Report the best solution
```

End

Algorithm 2. Pseudo code of the ACO algorithm

2.2 Genetic Algorithm

Darwin's theory about evolution inspired Holland and Goldberg [26,27]; they mimic natural evolution processes to find a solution to a problem: combination of selection, recombination and mutation. They form a subclass of evolutionary algorithms. Figure 1 illustrates its basic principle.



Fig. 1 The basic cycle of evolutionary algorithms

where Evaluation consists of computing the objective values of the solution candidates. Fitness Assignment uses the objective values to determine fitness values. Selection chooses the fittest individuals for reproduction, and Reproduction creates new individuals from the mating pool by crossover and mutation [28].

The pseudo code of a basic GA is given in Algorithm 3.

```
InitPopulation () // random initialization of the
population
     max fitness := 0
     For each member chromosome
           fitness := Fitness_Evaluation (chomosome)
               If fitness > max fitness
                       max_fitness := fitness
                       fittest solution = chromosome
               End
     End
     while generation < max_generations
               offspring := Selection (parents) // using
roulette-wheel selection
               fitness := Fitness_Evaluation (offspring)
               If fitness > max_fitness
                       max_fitness := fitness
                       fittest_solution = offspring
               End
     save fittest_solution
```

End

Algorithm 3. Pseudo code of the GA algorithm

2.3 Simulated Annealing

The method of simulated annealing (SA) was first introduced by Kirkpatrick [29]. This technique simulates the annealing process in which a solid, in a heat bath, is heated above its melting temperature and then progressively, the temperature is lowered slowly to produce the crystalline lattice, which reduces its energy probability distribution. This crystalline lattice is an attractive example of nature finding of an optimal configuration [30].

Generally, SA exploits the Metropolis Algorithm [31] which provides the criterion for acceptance of a solution 'x' constructed by disrupting the current solution x. This process gives the possibility of moving away occasionally of a local minimum to allow a widening of the research field of the ideal solution. There are several distinct steps that the SA process has to go through as the temperature is condensed and randomness is applied to the input values.

The pseudo code of the SA procedure is as follows:

```
Setup the SA.
Choose a random solution (x) which takes the
minimum solution x_{min} (x=x<sub>min</sub>)
Evaluate the cost function f(x) equal to f(x_{min})
Initialize the temperature T
Repeat
 Repeat
    Generate a neighbor X' perturbing the solution X.
       Acceptance with the criterion of Metropolis
       if f(x') \leq f(x)
          f(x) = f(x')
          x=x'
       if not
         Calculate \Delta f = f(x') - f(x)
         Calculate the probability p = \exp(-\Delta f/T)
         Choose a random solution R between [0, 1]
         if R \leq p
             f(x) = f(x')
            x = x'
         end if
         f_{min} = f(x) and x_{min} = x
       end if
  Until thermodynamic equilibrium reaches
T: = to decrease temperature
Until maximum iterations or minimum error criteria is
attained
```

Algorithm 4. Pseudo code of the SA algorithm

3 Test and application examples

Under similar conditions, the four metaheuristics were applied to the optimal design of the aforementioned two CMOS circuits and two test functions.

The proposed MATLAB-implemented algorithms parameters are given in Table 1 with a generation algorithm of 200 with Pentium (R) Dual-Core CPU, T4500 @2.3 GHz.

Table 1.	Parameters of algorithms

$\begin{array}{c c} \mathbf{O}_{\mathbf{A}} & \begin{array}{c} \text{inertia weight (w)} & 0.9 \\ \hline \text{Particle Velocity (c1)} & 1 \\ \hline \text{Particle Position (c2)} & 3 \\ \hline \text{Particle Position (c2)} & 3 \\ \hline \text{Particle Position (c2)} & 3 \\ \hline \hline \text{Particle Position (c2)} & 0.1 \\ \hline \hline \text{Quantity of Ants} & 1000 \\ \hline \hline \text{Quantity of deposit pheromone (Q)} & 0.2 \\ \hline \hline \text{Pheromone Factor (α)} & 1 \\ \hline \hline \text{Heuristics Factor (β)} & 1 \\ \hline \hline \text{Heuristics Factor (β)} & 1 \\ \hline \hline \text{Population size} & 1000 \\ \hline \hline \text{Crossover Probability} & 0.9 \\ \hline \text{Mutation Probability} & 1e-4 \\ \hline \hline \text{Initial temperature (T)} & 1000 \\ \hline \end{array}$			11115
$\begin{array}{c c} \mathbf{X} & \hline Particle \ Velocity \ (c1) & 1 \\ \hline Particle \ Position \ (c2) & 3 \\ \hline Particle \ Position \ (c2) & 3 \\ \hline \hline Particle \ Position \ (c2) & 3 \\ \hline \hline Particle \ Position \ (c2) & 3 \\ \hline \hline Particle \ Position \ (c2) & 3 \\ \hline \hline Population \ rate \ (\rho) & 0.1 \\ \hline \hline Quantity \ of \ Ants & 100 \\ \hline \hline Quantity \ of \ deposit \ pheromone \ (Q) & 0.2 \\ \hline Pheromone \ Factor \ (\alpha) & 1 \\ \hline Heuristics \ Factor \ (\beta) & 1 \\ \hline \hline Population \ size & 100 \\ \hline \hline Crossover \ Probability & 0.9 \\ \hline Mutation \ Probability & 1e-4 \\ \hline Initial \ temperature \ (T) & 100 \\ \hline \end{array}$		Swarm size	100
	Q	inertia weight (w)	0.9
$ \underbrace{ \begin{array}{c} & \underbrace{ \begin{array}{c} \text{Number of Ants} & 100 \\ \hline \text{Evaporation rate } (\rho) & 0.1 \\ \hline \text{Quantity of deposit pheromone } (Q) & 0.2 \\ \hline \text{Pheromone Factor } (\alpha) & 1 \\ \hline \text{Heuristics Factor } (\beta) & 1 \\ \hline \end{array} \\ \underbrace{ \begin{array}{c} \text{Population size} & 100 \\ \hline \text{Crossover Probability} & 0.9 \\ \hline \text{Mutation Probability} & 1e-4 \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} } $	PS	Particle Velocity (c1)	1
$ \begin{array}{c} \bullet \\ \bullet $		Particle Position (c2)	3
$\begin{array}{c c} & \hline & $		Number of Ants	100
$\begin{array}{c c} \hline Preforming Factor (\alpha) & 1 \\ \hline Heuristics Factor (\beta) & 1 \\ \hline \hline Population size & 100 \\ \hline \hline Crossover Probability & 0.9 \\ \hline Mutation Probability & 1e-4 \\ \hline Initial temperature (T) & 100 \\ \hline \end{array}$		Evaporation rate (ρ)	0.1
$\begin{array}{c c} \hline Preforming Factor (\alpha) & 1 \\ \hline Heuristics Factor (\beta) & 1 \\ \hline \hline Population size & 100 \\ \hline \hline Crossover Probability & 0.9 \\ \hline Mutation Probability & 1e-4 \\ \hline Initial temperature (T) & 100 \\ \hline \end{array}$	Ŭ	Quantity of deposit pheromone (Q)	0.2
Population size100Crossover Probability0.9Mutation Probability1e-4Initial temperature (T)100	A	Pheromone Factor (α)	1
Crossover Probability0.9Mutation Probability1e-4Initial temperature (T)100		Heuristics Factor (β)	1
Mutation Probability1e-4Initial temperature (T)100		Population size	100
Mutation Probability1e-4Initial temperature (T)100	P	Crossover Probability	0.9
		Mutation Probability	1e-4
▲ Annealing rate 0.9		Initial temperature (T)	100
S Ameaning rate 0.9	SA	Annealing rate	0.9
Final temperature 1e-8		Final temperature	1e-8

3.1 The test examples

In order to check the performances of the proposed algorithm, two classical objectives test functions [28,32] were used; their expressions are given in Table 2.

	Table 2. The test functions						
	Variable Bounds	Objective Functions					
F1	$-4 \le x, y \le 4$	$f(x, y) = (1.5 - x + xy)^2 + (2.25 - x + xy^2)^2 + (2.625 - x + xy^3)^2$					
F2	$0 \le x, y \le 10$	$f(x, y) = x\sin(4x) + 1.1y\sin(2y)$					

In Table 3 we present the obtained minimas by all the studied algorithm as well as the theoretical know results.

Table 3.	Comparison algorithm results and				
theoretical results					

	theoretical results	PSO	ACO	GA	SA			
F1	0.00	0.00	0.00	0.00	1.1581e-05			
F2	-18.5547	-18.5547	-18.5547	-18.5517	-18.5516			

We can notice that, the good agreement between theoretical results and those obtained using the proposed algorithms. The techniques ACO and PSO provide the global minima, whereas the GA and SA give closer but acceptable results.

3.2 The application examples

In the previous work, we have described our proposed algorithms and shown their performance on a set of well-known test functions. In this part, the abovementioned algorithms were used to optimize performances of the following analog circuits and performances under consideration are:

- The X-port parasitic resistance of a CMOS second generation current conveyor (CCII).
- The high cut-off frequency of a CMOS second generation current conveyor (CCII).
- The Open-loop voltage gain and the Common Mode Rejection Ratio, the Die Area and the Power dissipation of a two-stage CMOS Op-Amp.

3.2.1 Performance optimization of a CMOS CCII

The four considered techniques, i.e. PSO, ACO, GA and SA, were used to optimize performances of a CCII circuit that is shown on Figure 2.



Fig. 2 A second generation current conveyor (CCII)

3.2.1.1 Objective functions and constraints

The objective functions to be optimized are [33,34]:

- R_X : the X-port input parasitic resistance to be minimized.
- *fci*: the current high cut off frequency to be maximized.

All the CCII transistors must operate in the saturation mode. Saturation constraints of each MOSFET were determined [35].

The geometric variables to be considered for the CMOS CCII performances optimization are the MOS transistors sizes: channels lengths (LN, and LP) and gates widths (WN and WP) while respecting the saturation conditions of the MOS transistors. The used supply voltages are

 $V_{DD}/V_{SS}{=}2.5V/{-}2.5~V$ and a bias current, $I_{bias}{=}100~\mu A.$

3.2.1.2 Optimization results

Tables 4 and 5 give optimal results obtained by using the PSO, the ACO, the GA and the SA algorithms for the parameters and the circuit's performances for CCII.

Table 4. Optimization and simulation results for Rx_{min}

						min
	LN	WN	LP	WP	Rx_m	$i_n(\Omega)$
	(µm)	(µm)	(µm)	(µm)	Opt.	Sim.
PSO	0.59	18.74	0.35	30.00	464	477
ACO	0.55	20.36	0.36	30.00	441	451
GA	0.50	13.86	0.35	27.32	529	512
SA	0.55	17.49	0.35	30.00	473	475

Table 5. Optimization and simulation results for fci_m	Table 5.	Optimizatio	on and sim	nulation rea	sults for <i>fcima</i>	r
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	LN	WN	LP	WP	fci _{max}	(GHz)
	(µm)	(µm)	(µm)	(µm)	Opt.	Sim.
PSO	0.54	05.80	0.35	10.05	1.751	1.784
ACO	0.56	05.39	0.35	09.49	1.791	1.887
GA	0.58	5.96	0.36	10.56	1.576	1.621
SA	0.55	8.16	0.35	14.13	1.422	1.485

Figure 3 and 4 show the simulation results (Rx and fci) corresponding to the application of the PSO, ACO, GA and SA techniques for CCII.



Fig. 3 Rx-pole resistance (Ω) vs. frequency (Hz)



Fig. 4 Current gain (dB) vs. frequency (Hz)

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3.2.2 Optimizing performances of a CMOS operational amplifier

The schematic of the two stage CMOS operational amplifier is shown in Figure 5. Performances of the op-amp are evaluated via several parameters [10]:

- The Open-loop voltage gain Av to be maximized.
- The Common Mode Rejection Ratio *CMRR* to be maximized.
- The Die Area *A* to be minimized.
- The Power dissipation *P* to be minimized.



Fig. 5 A two stage CMOS operational amplifier

Determining the optimal dimensions of the transistors for a specific design involves a tradeoff among all these performance measures.

Ensuring the saturation of each transistor of the circuit constitutes the constraints of the problem [10].

The considered optimization problem is a multiobjective one that consists of maximizing two objective functions such as the Av, CMRR and minimizing the two other performances; the die area and the consumed power. In this work we focus on the mono-objective optimization. For this we will use the weighted cost functions technique [28]. It consists of weighting each function and transforming the set of objectives into an equivalent cost function (OF). Thus, OF can be expressed as follows:

 $OF = \alpha_1 A_{\nu} + \alpha_2 P + \alpha_3 A + \alpha_4 CMRR \tag{6}$

where α_{1-4} are normalization coefficients.

The compensation resistor ($R_c=800\Omega$), the compensation capacitor ($C_c=3pF$) and the capacitive load ($C_L=10pF$) are considered as fixed parameters. The transistors M1-M8 have a same channel length L but several gates widths W1-W8. Those

parameters and the bias current I_{bias} were optimized by the four algorithms. A Table 6 shows the obtained optimal values and the Table 7 gives the associate performances and simulations results.

Table 6. Optimization results

	W _{1,2} (μm)	W _{3,4} (μm)	W5 (μm)	W ₆ (μm)	W ₇ (μm)	W ₈ (μm)	L (µm)	Ιο (μΑ)
PSO	213.59	255.01	56.37	477.99	52.83	09.24	0.35	10.24
ACO	215.02	260.96	57.82	459.52	50.91	09.65	0.35	10.00
GA	211.49	260.09	79.42	404.09	61.69	09.52	0.35	10.16
SA	216.38	260.05	59.03	470.11	53.35	10.00	0.35	10.00

 Table 7. Performance and simulation results for

 Av, CMRR, A and P

		. , =	,		
		Av (dB)	CMRR (dB)	Α (μm ²)	P (mW)
PSO	Opt.	103.51	110.57	5368	1.3
P80	Sim.	095.43	101.43		1.8
ACO	Opt.	104.13	113.91	5354	1.2
ACO	Sim.	096.74	105.29		1.7
CA	Opt.	099.76	105.23	5242	1.6
GA	Sim.	092.86	096.58		2.4
SA	Opt.	104.50	108.35	5408	1.2
SA	Sim.	097.31	099.43		1.8

Figure 6 and 7 show the simulation results (*Av* and *CMRR*) corresponding to the application of the PSO, ACO, GA and SA techniques for Op-Amp.



Fig. 6 Gain (dB) vs. frequency (Hz)



Fig. 7 CMRR (dB) vs. frequency (Hz)

4 Computing time and Convergence checking

4.1 Computing time

Table 8 shows a comparison between average computing times for 100 runs of each algorithm. Figure 8 shows a recapitulation of the corresponding computing times.

Table 8.	Average computing time (seconds) for the
te	est functions and the studied circuits

Circuits and test functions	PSO	ACO	GA	SA
F1	0.1275	2.1392	0.1467	0.6753
F2	0.1628	2.4263	0.1563	0.9811
Rx	2.5876	7.2716	2.8982	4.0234
fci	2.4331	9.3154	2.5652	3.6842
Ampli-Op	4.3170	22.183	2.4972	3.1442



Fig. 8 Execution time (seconds) for the five objective problems

We clearly notice that the ACO algorithm is the slower compared to other algorithms.

4.2 Convergence checking

In order to check the convergence rate of the proposed algorithms, a robustness test was performed. i.e. the algorithms are applied a hundred times for optimizing all objectives (F1, F2, Rx, fc, Av, CMRR, P and S). In Figures 9, 10 and 11 we present the Box Plots of each algorithm for each objective considered function.



Fig. 9 Box plot for the convergence rate: (a) for F1 and (b) for F2 $\,$



Fig. 10 Box plot for the convergence rate: (a) for Rx and (b) for *fci*



Fig. 11 Box plot for the convergence rate: (a) for *Av*, (b) for *CMRR*, (c) for *P* and (d) for *A*

We can be easily noticed the good convergence ratio, despite the probabilistic aspect of the algorithms. We note that the spacing between the optimal values given by PSO and GA algorithms is larger than those of ACO and SA techniques which therefore show a good degree of dispersion. In the other hand, the PSO technique has the most outlier values and the GA presents the best symmetry of the values. We can, also, notice that the robustness of the ACO algorithm is better than the robustness of the PSO, GA and SA algorithms.

5 Conclusion

The presented work presents a comparison between four metaheuristic techniques: Particle Swarm Optimization, Ant Colony Optimization, Genetic and Simulated Annealing. Algorithm Each technique was first validated through mathematical test functions and used for the optimal sizing of two analog circuits; a CMOS second generation current conveyor and an operational amplifier. The considered algorithms achieve the optimal solution; the choice between these algorithms will depend on the desiderata of the designer. However, our results suggest that a hybrid algorithm consisting of at least two techniques, one taking care of optimum quality, the other taking care of running time, is a promising research direction.

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